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# A mechanistic model to predict droplet drying history and particle shell formation in multicomponent systems

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## Abstract

Spray drying allows tuning the physical properties of the resulting powders widely. However, targeted process design is complicated by the interplay between process characteristics and the non-ideal physical properties exhibited by multicomponent mixtures, such as pharmaceutical formulations. This work presents a mechanistic model describing the drying of single droplets. The model includes heat and mass balances, non-ideal vapour-liquid equilibria, and population balances describing the evolution of particulates within the drying droplet. The model is applied to (up to) ternary mixtures of solvents, polymers and solutes, and predicts properties of the drying droplet such as the time of shell formation and the size of the particle obtained after drying. A comparison with experimental data from single droplet drying experiments carried out at defined relative vapour saturation and temperature shows that the model can be used to predict shell formation (as well as other properties) for the systems studied here.

*Keywords:* spray drying; single droplet drying; acoustic levitation; non-ideal multicomponent systems; mechanistic population balance equation model

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## 10 **1. Introduction**

11 The concept of engineering materials to improve functionality is widely applied in many industries  
12 where relationships between structure and functional properties are of vital importance [1, 2]. In the  
13 pharmaceutical industry, formulating active pharmaceutical ingredients (APIs) often requires physio-  
14 chemical protection of the API and API release modulation in addition to chemical/physical modifica-  
15 tions for efficient drug delivery. As such, the development of highly engineered micro and nanoparticle  
16 matrices has become critical for use in drug delivery technologies [3, 4]. Spray drying offers an op-  
17 portunity to design such particles in a single step involving simultaneous drying and particle formation  
18 from droplets containing API, excipient and solvent either in the form of a solution or a suspension. It  
19 has gained wide acceptance in the pharmaceutical industry as an effective method for the production of  
20 amorphous API-excipient matrices due to the rapid evaporation of solvent, thereby directly increasing  
21 the dissolution rate of many insoluble drugs [3, 5–7]. Spray drying involves first the atomisation of a  
22 liquid or suspension into droplets, typically with sizes between 10 and 100  $\mu\text{m}$ , followed by solvent  
23 evaporation through convective heating leading to particle formation and subsequent drying. The large  
24 surface area created by atomisation allows the drying process and particle formation to occur rapidly  
25 and simultaneously [7, 8].

26 By controlling process conditions and formulation properties, the particles produced can be typically  
27 tailored for use in oral and pulmonary drug delivery systems. Each of these applications requires par-  
28 ticles with different physical characteristics such as size, bulk density and porosity [9, 10]. Predicting  
29 such product characteristics is difficult due to the strong coupling between atomisation, drying and par-  
30 ticle formation [7]. In addition, particle characteristics can impact the ease at which post-processing  
31 stages such as tableting are accomplished and as such, a deeper understanding of the processes leading  
32 to particle formation is required. In general, experimental investigations carried out at scale can be  
33 time-consuming and material intensive. Therefore, developing appropriate modelling methodologies  
34 to predict such varying product characteristics can be highly valuable.

35 Theoretical models that predict particle morphologies and process behaviour require an adequate de-  
36 scription of the drying kinetics of droplets, which in turn become wet and then dry particles. In order  
37 to validate such models, access to insightful experimental data is required. However, it is difficult to

38 precisely follow the evolution of droplets/particles in an actual spray drying process, because there  
39 are typically millions of rapidly drying droplets simultaneously present in the spray drying chamber.  
40 Therefore, several attempts have been made to develop comparable experimental and theoretical meth-  
41 ods based on single droplet drying (SDD) approaches. Although, inter-droplet effects are ignored in  
42 SDD methods, they are useful to understand process behaviour and for validation of modelling method-  
43 ologies [11, 12]. Experimental and model attempts have been described and summarised in several  
44 review articles [11, 13–17]. Although several modelling methodologies have been well described, they  
45 are still limited, particularly with respect to their treatment of non-ideal and multicomponent systems.  
46 The droplet drying process is often separated into two main drying regimes. The first drying stage,  
47 where the droplet is still completely covered with the liquid phase and the second drying stage where  
48 a solid shell is present. In reality, formulations subjected to spray drying are often complex multi-  
49 component systems. A detailed overview of theoretical methods is given in a review by Mezhericher  
50 et al. [18]. Until now, the most advanced of these combine mass and energy balances with a population  
51 balance approach to describe the entire droplet drying history; including the mechanisms of particle  
52 formation (nucleation and growth) [19–21]. This allows for a complete mechanistic description of the  
53 processes occurring within the droplet domain. Such models thus require the solution of a set of partial  
54 differential equations describing heat and mass transport as well as fluid mechanics within a moving  
55 domain. Although this is computationally intensive, the approach can capture the main drying be-  
56 haviour. Seydel et al. [21] described a binary solution using a 1D population balance model to describe  
57 the crystallisation of individual particles within the drying droplet. This was combined with equations  
58 to describe the evolution of concentration and droplet surface temperature during drying. The model  
59 was based on several assumptions that includes ideal vapour-liquid equilibrium and spherical symmetry  
60 of the droplet. In the second drying stage, the critical point of the shell was identified at a predefined  
61 solid fraction at the droplet surface and drying was assumed to proceed in a funicular manner (dry-  
62 shell route) where the evaporation front recedes into the recess of the formed particle. Experimental  
63 results were used to validate the physical processes leading to particle formation and a good agreement  
64 was obtained. More recently, Handscomb et al. [19, 20] extended the model of Seydel et al. [21] to  
65 predict the structural evolution of an ideal binary droplet containing suspended solids. The continuous  
66 and discrete phases were similarly described, with the critical point identified by a predetermined solid  
67 volume fraction. The droplet temperature was assumed to be uniform in both drying stages. The model

68 however included a shell thickening regime such that droplet shrinkage can continue from the point at  
69 which the initial shell is formed to when the shell becomes strong enough to withstand external pressure  
70 exerted on the shell surface. This was coupled with a known dry shell model, and a model involving  
71 the presence of a bubble (wet shell). It has been postulated that such sub-models for the second drying  
72 stage (wet shell, dry shell, etc.) present the key to developing a comprehensive model for spray dryers  
73 [10, 22]. The drying history prior to shell formation has been shown to determine events leading to  
74 the use of the several sub-models [22]. Although previous researchers have developed powerful insight  
75 into describing particle morphologies, the models until now have limited validation and applicability,  
76 particularly in the context of complex multicomponent formulations.

77 In the present work, an extensive evaporation and particle formation model is used to describe drying  
78 prior to shell formation in multicomponent systems. The model incorporates population balance equa-  
79 tions to describe the evolution of the particle size distribution (PSD) within each part of the domain.  
80 Unlike previous models where shell formation is activated through a predetermined solid fraction, infor-  
81 mation obtained from the PSD is used to describe shell formation directly. The assumptions of uniform  
82 droplet temperature is relaxed. Although, Farid [23] shows that this assumption is appropriate during  
83 the initial phase of drying, the distribution during the later phase of drying (following shell formation),  
84 or in systems where thermal conductivity in different phases varies by some order of magnitude cannot  
85 be ignored. The evaporation phenomenon is described in a more sophisticated manner than in previous  
86 works [19–21], accounting for non-ideality of mixtures and the effect of Stefan flow (due to moving  
87 droplet boundary) within the droplet. Overall, the model combines some features of previous works  
88 in this area, but it is extended to multicomponent mixtures with considerable non-ideality in order to  
89 describe typical pharmaceutical formulations. In the work that follows, a model describing the drying  
90 process up to the point of shell formation (i.e., the critical point) is discussed. A model for the second  
91 drying stage, i.e., after shell formation, will form the subject of future work. The remainder of this  
92 work is structured as follows: in Section 2, a theoretical understanding of droplet drying kinetics and  
93 particle formation is explored. In Section 3, model equations are formulated that describe transport  
94 of mass and energy within the droplet and between the droplet and gas phase, as well as the growth  
95 and nucleation of individual particles within the droplet. In Section 4, the numerical implementation  
96 of the moving boundary problem is discussed. In Section 5, the experimental methods used for model

97 validation are discussed and in Section 6, the effect of drying condition on droplet drying kinetics is  
98 discussed in detail and relevant conclusions are made in Section 7.

## 99 **2. Drying process and particle morphologies**

100 Before entering into the description of the model, it is useful to summarise the physics and mechanisms  
101 involved in droplet drying. Ranz and Marshall [24] and Charlesworth and Marshall [25] provided a de-  
102 tailed experimental and theoretical basis for the drying history of droplets containing solutes. Initially,  
103 concentration gradients are established within the droplet due to solvent evaporation at the droplet sur-  
104 face. This leads to solvent migrating towards the surface and solutes moving towards the centre due to  
105 diffusion. The extent of the gradient is the result of the drying kinetics ensuing at different temperature,  
106 relative saturation of the gas phase and composition of the liquid phase. The drying history of a droplet  
107 containing a solution can be well summarised with a temperature versus time curve (Figure 1) [26]. In  
108 the initial stage of drying, the droplet is rapidly heated to the wet bulb temperature (A-B). As long as  
109 the droplet surface is saturated with moisture the temperature remains constant with drying proceed-  
110 ing at a near constant rate (B-C). This period of drying is easily identified by the shrinking of droplet  
111 diameter. At the critical point there is insufficient moisture to maintain the surface saturation, the tem-  
112 perature starts to rise until it reaches the boiling point of the liquid (C-D) where vaporisation (above  
113 boiling point) begins. At this point, ideal shrinkage ceases. This phase coincides with the formation  
114 of a shell/crust at the outer layer of the droplet, and drying changes from being surface evaporation  
115 controlled to being controlled by internal moisture migration. In Figure 1, a shell is formed somewhere  
116 between point C and D. During boiling, a considerable amount of energy is required in the form of  
117 latent heat of vaporisation, therefore the sensible heating of the droplet/particle halts and drying is con-  
118 trolled solely by external heat transfer (D-E). Once the moisture removal is complete, the temperature  
119 of the particle rises until it thermally equilibrates with the surrounding gas temperature [26, 27]. In  
120 many industrial drying processes, drying is often terminated before point D (i.e., boiling of the solvent)  
121 since this necessitates significant energy requirements as well as appropriate process residence times.  
122 Depending on the droplet drying history, a range of particle morphologies can be obtained at the end of  
123 drying [28]. Several authors have given an account of the complex intra-droplet transport phenomena  
124 using single droplet drying studies. This has led to the classification of different particle morphologies

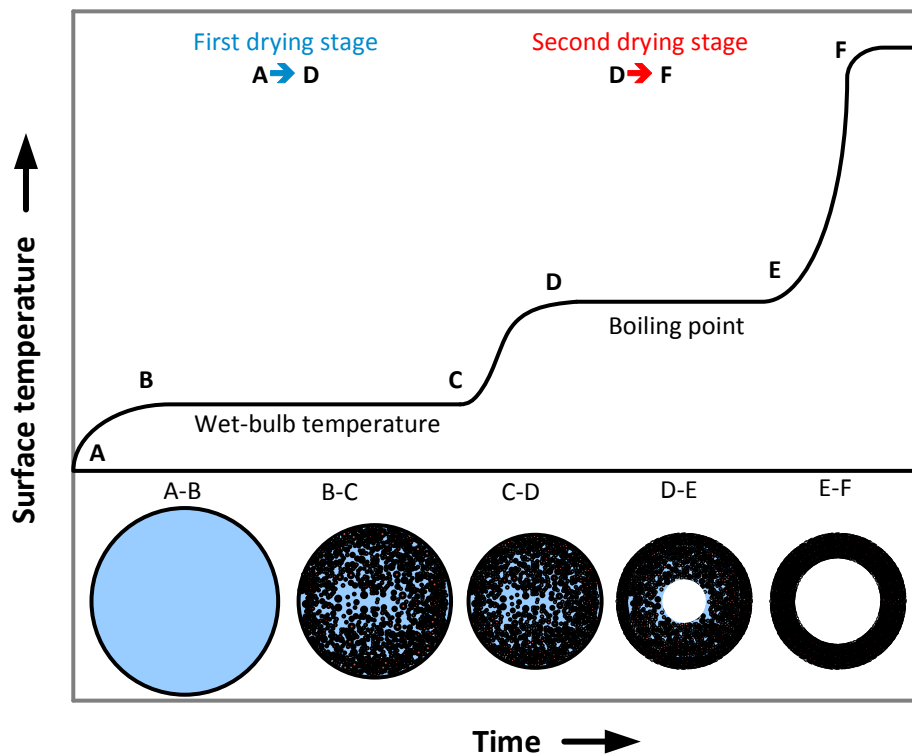


Figure 1: A typical droplet/particle surface temperature profile. At the bottom, one characteristic type of particle morphology is shown; an overview of other attainable morphologies is given in Figure 2.

125 obtainable when droplets are spray dried [10, 28]. The different obtainable particle morphologies are  
 126 illustrated in Figure 2. When drying is slow, there is sufficient time for the equilibration of concentra-  
 127 tion gradients. In this case the Peclet number,  $Pe$  defined as the ratio of convective to diffusive transport  
 128 is small. This leads to a (close to) uniform droplet and eventually a solid rigid porous structure. When  
 129 drying is fast (i.e. large Peclet number), there is little time for diffusion to occur, leading to large con-  
 130 centration gradients between the surface and the centre of the droplet. This may lead to the formation  
 131 of a variety of complex morphologies for the dried particle. For instance, the formation of a vapour  
 132 bubble within the droplet can occur due to sudden pressure gradients. This can lead to a cycle of in-  
 133 flation and deflation of the forming particle and subsequently formation of rigid hollow structures. In  
 134 such a case, particles may also deform to produce structures that are cracked or shrivelled (Figure 2).

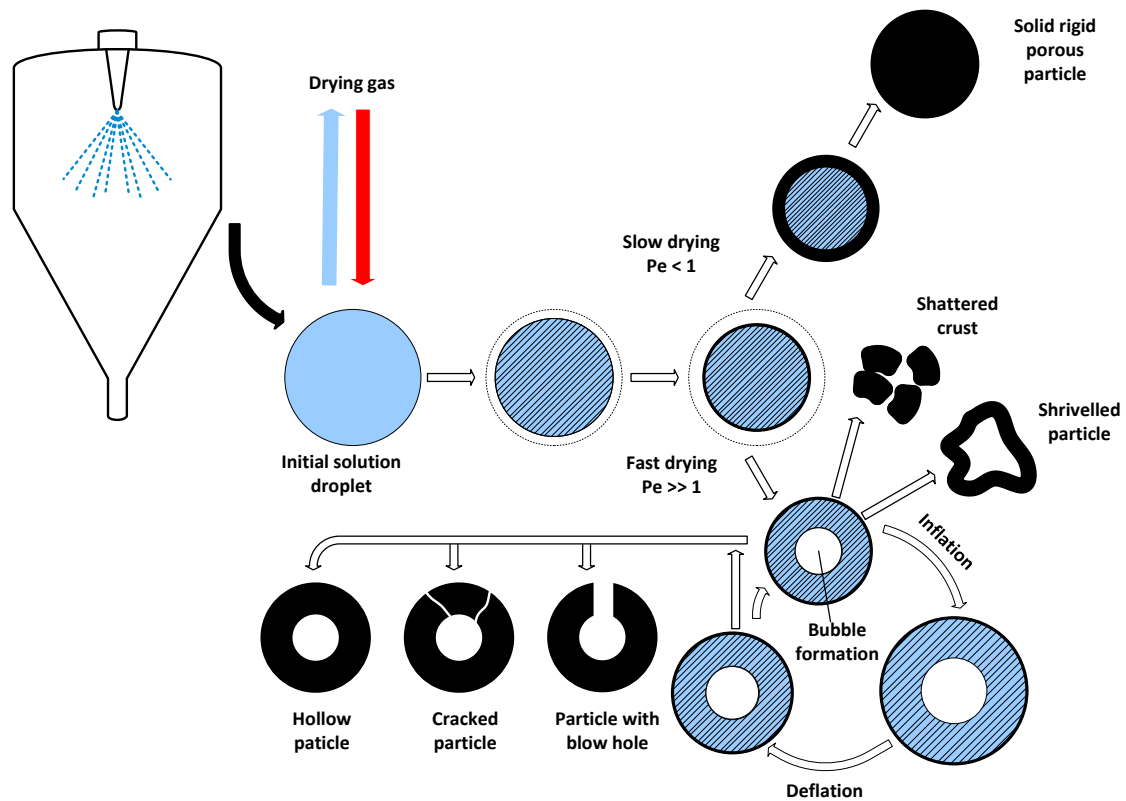


Figure 2: Examples of possible morphological evolutions of a solution droplet during drying. This work focuses on the evolution of the droplet/ particle up to the point where the shell is formed.

### 135 3. Model Formulation

#### 136 3.1. Prior to Shell formation

137 In the drying of a droplet containing two or more species of dissolved solutes, the solute molecules  
 138 move simultaneously relative to each other by advection and diffusion in the continuous liquid phase, as  
 139 the droplet shrinks due to solvent evaporation. This leads to concentration gradients, with particularly  
 140 high concentrations occurring at the droplet surface. If the concentration exceeds the solubility limit,  
 141 i.e., is higher than the equilibrium concentration at a given temperature and pressure, a driving force  
 142 for crystallisation exists. This driving force, commonly expressed as supersaturation, i.e., the ratio of  
 143 actual concentration and the equilibrium concentration at a given time and position, leads to nucleation  
 144 (increase in number) and growth (increase in size) of particulates in the solution. This in turn leads to a  
 145 rapid increase in the total solid fraction of particulates within the droplet, which ultimately leads to the



161 diffusion [29]. Writing a mass conservation equation on the control volume shown in Figure 3, the  
 162 evolution of specie concentration in the droplet over time can be described;

$$\frac{\partial c_i}{\partial t} = -\frac{1}{r^2} \frac{\partial}{\partial r} (r^2 u^{(C)} c_i) + \frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 \sum_{j=1}^{n-1} D_{ij}^{(C)} \frac{\partial c_j}{\partial r} \right) - \rho_i^{(D)} \frac{\partial \varepsilon_i}{\partial t} \quad (1)$$

163 where  $i = 1, 2, \dots, n - 1$  for an  $n$  component system. The first and second term on the right hand side  
 164 are mass transport terms due to advection and diffusion, respectively, while the last term describes  
 165 the mass of solute consumed for nucleation and growth of particles from the solution.  $c_i$  denotes the  
 166 concentration of component  $i$ , defined by  $c_i = \rho^{(C)} w_i (1 - \varepsilon)$ .  $\rho^{(C)}$  is the density of the continuous phase,  
 167  $w_i$  is the mass fraction of component  $i$  in the continuous phase,  $\varepsilon$  is the solid fraction,  $t$  is time,  $r$  is the  
 168 spatial radial coordinate,  $u$  is the diffusion dependent advective velocity and  $D_{ij}$  are multicomponent  
 169 diffusion coefficients. This equation is valid from the centre of the droplet ( $r = 0$ ) to the surface of the  
 170 droplet ( $r = r_s$ ). The value of  $\varepsilon$  can be obtained from:

$$\frac{\partial \varepsilon_i}{\partial t} = k_{vi} \frac{\partial \mu_{3i}}{\partial t} = k_{vi} \frac{\partial}{\partial t} \int_0^\infty N_i L^3 dL \quad (2)$$

171 where  $k_v$  is a shape factor relating the volume of a particle to the cube of its characteristic size. This  
 172 means that  $k_v = 1$  for cubes,  $k_v = \pi/6$  for spheres and  $k_v \ll 1$  for needles (when the characteristic size  
 173 of the needles is their length).  $\mu_3$  is the third moment of the PSD,  $\rho_i^{(D)}$  is the density of the crystal,  $N_i$  is  
 174 the PSD (number of particles per total volume per particle size) and  $L$  is the characteristic size (length)  
 175 of the particles.

176 The following dependencies of the different quantities exist:

$$177 \quad \mathbf{c} = \mathbf{c}(t, r), \boldsymbol{\rho}^{(C)} = \boldsymbol{\rho}^{(C)}(c, T), \mathbf{T} = \mathbf{T}(t, r), \boldsymbol{\varepsilon} = \boldsymbol{\varepsilon}(t, r)$$

$$178 \quad \mathbf{u} = \mathbf{u}(c), \mathbf{D} = \mathbf{D}(\eta, T) \boldsymbol{\eta} = \boldsymbol{\eta}(c, T) \mathbf{N} = \mathbf{N}(t, r, L)$$

179 where  $\eta$  is the dynamic viscosity of the liquid and  $T$  is the droplet temperature.

180 In general, the diffusion coefficients in a multicomponent system are not symmetrical (i.e.  $D_{ij} \neq$   
 181  $D_{ji}$ ). This implies that the flux of one component is related to the concentration gradient of  $(n - 1)$

182 solutes, where one component is designated as the solvent. Hence in an  $n$ -component system,  $(n - 1)^2$   
 183 independent diffusion coefficients are required to describe the system, where the value of the main  
 184 coefficients ( $D_{i,j,i=j}$ ) are similar to that in a binary solution. The cross coefficients ( $D_{i,j,i \neq j}$ ) can however  
 185 be significantly lower. Values of these diffusion coefficients are preferably obtained experimentally.  
 186 In order to write an expression for the diffusion dependent advective velocity, the volume fluxes are  
 187 assumed to be as in an ideal system and the volume average advective velocity can be written in terms  
 188 of specie concentration as [29]:

$$u^{(C)} = D_{12} \frac{\rho_1 - \rho_2}{\rho_1 \rho_2 - \rho_2 c_1 + \rho_1 c_1} \frac{\partial c_1}{\partial r} \quad (3)$$

189 Eq. (1) is complemented by the following boundary conditions:

190 Symmetry is assumed at the centre of the droplet

$$\frac{\partial c_i}{\partial r} = 0 \quad \text{at} \quad r = 0 \quad (4a)$$

191 and a defined evaporative flux at the droplet surface

$$-u^{(C)} c_i + \sum_{j=1}^{n-1} D_{ij}^{(C)} \frac{\partial c_j}{\partial r} = \delta_i \frac{\dot{m}_{v,i}}{4\pi r^2} \quad \text{at} \quad r = r_s \quad (4b)$$

192 where  $\delta_i$  is 1 for the evaporating component(s), 0 for the non-evaporating component(s) in Eq. (4b),  
 193 and  $\dot{m}_{v,i}$  denotes the mass vaporisation rate of component  $i$ .

### 194 3.1.2. Discrete phase model

195 In a similar manner, a conservation equation can be written to describe the evolution of particles within  
 196 the control volume. The solid phase evolves in the spatial domain through advection/diffusion and in  
 197 the internal particle length coordinate through nucleation/growth. The change in number density of  
 198 particles resulting from this can be written as:

$$\frac{\partial N_i}{\partial t} = -\frac{1}{r^2} \frac{\partial}{\partial r} (r^2 u^{(D)} N_i) + \frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 \sum_{j=1}^{n-1} D_{ij}^{(D)} \frac{\partial N_j}{\partial r} \right) - \frac{\partial (G_i N_i)}{\partial L} \quad (5)$$

199 where  $G$  is the particle growth rate (i.e., the increase in the size of the particulates with time) and is a  
 200 function of the supersaturation of the solution.

201 Eq. (5) exists in two coordinates and thus the solution to the partial differential equation requires two  
 202 boundary conditions each for the radial and particle size coordinates (for each particle forming compo-  
 203 nent). In the radial coordinate,  $r$  the boundary condition is that of symmetry and no flux of particles at  
 204 the droplet centre and surface respectively:

$$\frac{\partial N_i}{\partial r} = 0 \quad \text{at } r = 0 \quad (6a)$$

205

$$-u^{(D)}N_i + \sum_{j=1}^{n-1} D_{ij}^{(D)} \frac{\partial N_j}{\partial r} = 0 \quad \text{at } r = r_s \quad (6b)$$

206 In the particle size coordinate,  $L$  the first boundary condition accounts for the nucleation of particles.  
 207 The second condition is that no infinitely sized particles exist. This is written mathematically as:

$$G_i N_i(t, r, L) = J_i \quad \text{at } L = L_{min} \quad (6c)$$

208

$$N_i(t, r, L) = 0 \quad \text{at } L = \infty \quad (6d)$$

209 The rate of nucleation  $J$  and subsequent growth  $G$  of the crystals are described by the empirical func-  
 210 tional forms:

$$J_i = A_i \exp\left(\frac{B_i}{\ln^2 S_i}\right) \quad (7)$$

$$G_i = k_{gi} (S_i - 1)^{\alpha_i} \quad (8)$$

211 where  $S$  is the supersaturation ratio ( $c/c_{sat}$ ), and  $A$ ,  $B$ ,  $k_g$  and  $\alpha$  are material dependent kinetic/thermodynamic  
 212 parameters. The values of these constants for the model substances used in this work are given in the  
 213 results section.

214 *3.1.3. Droplet heat transport model*

215 In addition to the mass conservation equations, an energy balance is required to describe the tempera-  
 216 ture distribution within the drying droplet. The transport of energy is similarly given by convection and  
 217 conduction:

$$\frac{\partial}{\partial t}(\rho C_p T) = -\frac{1}{r^2} \frac{\partial}{\partial r}(r^2 u \rho C_p T) + \frac{1}{r^2} \frac{\partial}{\partial r}(r^2 \lambda \frac{\partial T}{\partial r}) - \sum_j^{n-1} \rho_j^{(D)} \Delta H_{\text{crys},j} \frac{\partial \varepsilon_j}{\partial t} \quad (9)$$

218 where  $C_p$  is the overall specific heat capacity and  $\lambda$  is the thermal conductivity of the suspension  
 219 estimated as a weighted average (cf. supporting information) and  $\Delta H_{\text{crys}}$  is the energy released by  
 220 crystallisation.

221 This is complemented by the boundary conditions. Symmetry at the centre of the droplet:

$$\frac{\partial T}{\partial r} = 0 \quad \text{at} \quad r = 0 \quad (10a)$$

222 Assuming heat transfer to the droplet surface is by convection from the ambient gas, the boundary  
 223 condition at the surface can be written as;

$$-u \rho C_p T + \lambda \frac{\partial T}{\partial r} = \frac{\dot{Q}_{\text{in}} - \dot{H}_{\text{out}}}{4\pi r^2} \quad \text{at} \quad r = r_s \quad (10b)$$

224 The above equation at the boundary represents the balance in energy required to heat up and evaporate  
 225 the droplet ( $\dot{Q}_{\text{in}}$ ), and the energy of the liquid evaporating from the surface ( $\dot{H}_{\text{out}}$ ).

226 *3.1.4. External heat and mass transport model*

227 The evaporation process is modelled using the original Abramzon and Sirignano [30] model. The  
 228 evaporation phenomenon is described with some assumptions. This include negligible gas solubility  
 229 in the liquid phase, no heat transfer by radiation and that mass transport occurs through a gas/liquid  
 230 film at the droplet boundary layer. A mass balance for liquid/vapour across the interface yields the  
 231 instantaneous evaporation rate  $\dot{m}_v$ . When modified for a multicomponent system [31],  $\dot{m}_v$  is written as

232 the sum of each evaporating component as:

$$\dot{m}_v = \sum_i 2\pi\rho_{i,v}D_{i,v}R_i\widehat{Sh}_i \ln(1 + B_{M,i}) \quad \text{for } Re \leq 400. \quad (11)$$

233 where  $\rho_{i,v}$  and  $D_{i,v}$  are the average density and vapour diffusivity of the  $i$ th component in the film  
 234 respectively.  $R_i$  is the volume-equivalent partial radius,  $\widehat{Sh}$  is the modified Sherwood number  $\widehat{Sh} =$   
 235  $2 + (Sh - 2)/F_M$ ,  $F_M$  is a film correction factor accounting for the effect of surface blowing  $F_M =$   
 236  $(1 + B_M)^{0.7} \ln(1 + B_M) / B_M$ ,  $Sh = 1 + (1 + Re Sc)^{1/3} f(Re)$  is the actual Sherwood number [32], and  
 237  $f(Re) = 1$  for  $Re \leq 1$  and  $f(Re) = Re^{0.077}$  for  $Re \leq 400$ .  $B_{M,i}$  is the Spalding mass transfer coefficient  
 238 and  $Re$  ( $Re = 2\rho r_s/\eta$ ) is the dimensionless Reynolds number [30].

239 The value of  $R_i$  is calculated using the volume fraction of the evaporating component [27, 33].

$$R_i = r_s \left( \frac{V_i}{\sum_{i=1}^n V_i} \right)^{\frac{1}{3}} \quad (12)$$

240 where  $r_s$  is the droplet/particle radius and  $V_i$  is the partial volume of component  $i$ . The driving force  
 241 for evaporation,  $B_{M,i}$  is calculated from;

$$B_{M,i} = \frac{w_{i,s} - w_{i,\infty}}{1 - w_{i,s}} \quad (13)$$

242 where  $w_{i,s}$  and  $w_{i,\infty}$  are the vapour mass fractions of the evaporating component at the surface and in  
 243 the bulk gas respectively.

244 It is also possible to write a balance for the rate of heat transferred to the droplet, where the heat  
 245 transferred is used to heat up the droplet and evaporate the solvent. This is written as:

$$\dot{Q}_{in} = \dot{m}_v \left( \frac{C_{pv}(T_\infty - T_s)}{B_{Ti}} - \Delta h_{fg}(T_s) \right) \quad (14)$$

246 where  $B_{Ti}$  is the heat transfer number given by: [30].

$$B_{Ti} = (1 + B_{Mi})^{\psi_i} - 1 \quad (15)$$

247 and  $\psi$  in the above expression is:

$$\psi = \frac{C_{pv}}{C_{pg}} \left( \frac{\bar{Sh}}{\bar{Nu}} \right) \frac{1}{Le} \quad (16)$$

248 where  $Le$  is the dimensionless Lewis number ( $Le = \lambda_g / (\rho_g D_g C_{pg})$ ).

### 249 3.1.5. Phase Behaviour

250 Evaporation of a droplet is a two phase problem and hence, equations describing the two phases (liquid  
251 and gas) must be solved. In addition, one needs to describe the thermodynamic equilibrium between  
252 the gas and liquid phases at the interface. The description of the liquid and gas phases have been de-  
253 scribed in Section 3.1.1 and Section 3.1.4 respectively. Since the presence of additional components  
254 within a liquid mixture can influence the vapour pressure of the liquid at the droplet surface and hence  
255 the degree of solvent flux during evaporation, it is also necessary to describe the thermodynamics at  
256 the liquid-vapour interface [29]. The description of thermodynamic equilibrium is often well repre-  
257 sented by the modified Raoult's law  $P_i = x_i \gamma_i P_{i,sat}$ . Here, the effect of liquid phase non-ideality in a  
258 mixture is accounted for using the activity coefficient  $\gamma_i$ . These can be described using a variety of  
259 models. In complex systems such as organic solutions, group contribution methods such as UNIFAC  
260 provide a useful and often reliable way of predicting the non-ideal liquid behaviour. For this work,  
261 pure component physical properties and correlations are obtained from a range of sources (values are  
262 tabulated in Table 2) [34, 35]. For mixtures, composition dependent correlations are used as detailed in  
263 the supporting documentation.

### 264 3.2. Shell formation

265 Although the model described in Section 3.1 is only valid prior to shell formation, the concept and  
266 equations are similarly applicable during and after shell formation. The shell is deemed to form at  
267 a critical point, where the solid particles are unable to move sufficiently relative to each other. This  
268 critical point is affected by the properties of the particles forming the shell. Eq. (17) therefore relates  
269 the critical solid fraction  $\varepsilon_{crit}$  for a stable packing as a function of the width of the PSD (using the mass  
270 weighted geometric standard deviation  $\sigma_g$  of the PSD). The original version of this equation [36] fitted  
271 for particles with sphericity of 0.81 and 0.86 is extrapolated for the needle like crystals of the model

272 compound used in this work (D-mannitol). An aspect ratio of 8 is selected to describe the needle-like  
 273 crystals [37]. This gives a sphericity of 0.69 [38] (assuming the needle-like shapes are well described  
 274 as cylindrical rods) - c.f. supporting information).

$$\varepsilon_{crit} = 0.7694 - 0.524/\sigma_g \quad (17)$$

275 This critical solid fraction is always reached first at the surface of the droplet, because supersaturation is  
 276 at its maximum there, which causes increased particle formation and growth and therefore a higher solid  
 277 fraction at the surface. The formation of a shell (somewhere between point C and D in Figure 1) starts  
 278 when the simulated solid fraction at the surface reaches the critical solid fraction given by Eq. (17).

#### 279 4. Numerical Implementation

280 To solve the moving boundary problem, a coordinate transformation is applied to render the boundary  
 281 positions fixed. This way, the wealth of methods available in literature for solving fixed boundary  
 282 problems can be applied. The radial coordinate of the droplet is transformed through normalisation  
 283 into the new spatial coordinate,  $\tilde{r} \in [0 \ 1]$  [21]. The transformation reads:

$$\tilde{r} = \frac{r}{r_s(t)} \quad (18)$$

284 The following partial differential relations can be derived [21].

$$\frac{\partial}{\partial r} = \frac{\partial \tilde{r}}{\partial r} \frac{\partial}{\partial \tilde{r}} = \frac{1}{r_s(t)} \frac{\partial}{\partial \tilde{r}} \quad (19)$$

$$\frac{\partial^2}{\partial r^2} = \left( \frac{\partial \tilde{r}}{\partial r} \right)^2 \frac{\partial^2}{\partial \tilde{r}^2} = \frac{1}{r_s(t)^2} \frac{\partial^2}{\partial \tilde{r}^2} \quad (20)$$

$$\frac{\partial}{\partial t} \Big|_r = \frac{\partial \tilde{r}}{\partial t} \frac{\partial}{\partial \tilde{r}} + \frac{\partial}{\partial t} \Big|_{\tilde{r}} = -\frac{\tilde{r}}{r_s(t)} \frac{dr_s}{dt} \frac{\partial}{\partial \tilde{r}} + \frac{\partial}{\partial t} \Big|_{\tilde{r}} \quad (21)$$

287 As seen in Eq. (21), the partial differential equation in the newly transformed coordinate includes  
 288 a virtual flux term that incorporates a velocity due to shrinkage. The liquid phase, solid phase and  
 289 energy equations are solved using the finite volume scheme [39]. This converts the partial differential

290 equations into ordinary differential equations (ODEs) that are coupled with the gas phase equation. The  
291 ODEs are solved numerically using a high resolution scheme, where upwind numerical flux functions  
292 are evaluated using the method detailed by Koren [40]. Although the order of accuracy can vary  
293 depending on the profiles simulated, the scheme is numerically stable as proven by Koren [40]. Very  
294 steep gradients lead to first order accuracy  $O(h)$  (where  $h$  is the step size in the grid), while smooth  
295 regions can have up to third order accurate solutions  $O(h^3)$ . This means that the error scales with the  
296 width of the discretization step in the particle size ( $L$ ) and radial coordinate ( $r$ ) with the mentioned  
297 orders. Since the physics of droplet drying involves phenomena that introduce sharp gradients (caused  
298 by the shrinkage in  $r$  and the nucleation in the  $L$  coordinate) and phenomena that smooth out gradients  
299 (diffusion), the actual order of accuracy of the solution to the system of equations is between first order  
300  $O(h)$  and third order  $(O)h^3$ . For the simulations discussed here, a semi discrete scheme is employed,  
301 where the number of grids is selected based on the convergence behaviour of the mixture simulated in  
302 order to yield good accuracy. Note that depending of the system simulated, this sometimes necessitates  
303 the use of a non-uniform grid in space. A grid size of 100 is used in the simulations shown here.  
304 Accuracy and convergence studies (see supporting documentation) show that the solution obtained in  
305 this work is near  $(O)h^2$ . In the time domain, the system of ODEs is solved using established ODE  
306 solvers; in this case Matlab's ODE45 [41], with absolute and relative error tolerance levels of  $10^{-8}$ .

## 307 **5. Experimental study**

### 308 *5.1. Materials*

309 PVP (K-30) and D-mannitol at purity >99% were obtained from Sigma Aldrich and Alfa Aesar respec-  
310 tively. Ultra pure water with resistivity of 19 M $\Omega$ .cm was obtained from a Direct-Q3UV purification  
311 system from Merck and was used for the preparation of all aqueous solutions.

### 312 *5.2. Experimental Setup*

313 A single droplet drying setup similar to that first described by Yarin et al. [14] is used to emulate the  
314 drying conditions. Here, a conditioned gas is introduced with controlled gas flow rate, temperature and

315 humidity around the droplet (see Figure 4). This setup is used to follow the evaporation of the single  
316 droplet by measuring its size with a camera. The inner diameter of the acoustic levitation chamber is  
317 70 mm, with two sealable access windows of diameter 25 mm. The windows allow access for optical  
318 imaging and droplet suspension in the acoustic field. The set-up consists of a 100 kHz ultrasonic  
319 droplet levitator (Tec5, Germany), a camera (Allied Vision Manta G505B), backlight illumination and  
320 a controlled evaporator unit (Bronkhorst, CEM 202A). The levitator chamber is surrounded by a heating  
321 jacket as shown in Figure 4. In this apparatus, the evaporator mixer is used to supply the chamber with a  
322 controlled gas flow at desired conditions (gas velocity, temperature, relative humidity). The evaporator  
323 mixer takes nitrogen gas and solvent flows from a gas cylinder and liquid tank. In the evaporator,  
324 the liquid and gas components are mixed and heated up to create the desired gas conditions. This is  
325 then sent to the levitator, surrounded by a heating jacket to maintain chamber conditions. A droplet is  
326 placed in the levitator using a Hamilton 1800 syringe and is suspended against gravity by means of a  
supporting ultrasonic sound pressure generated by a standing wave.

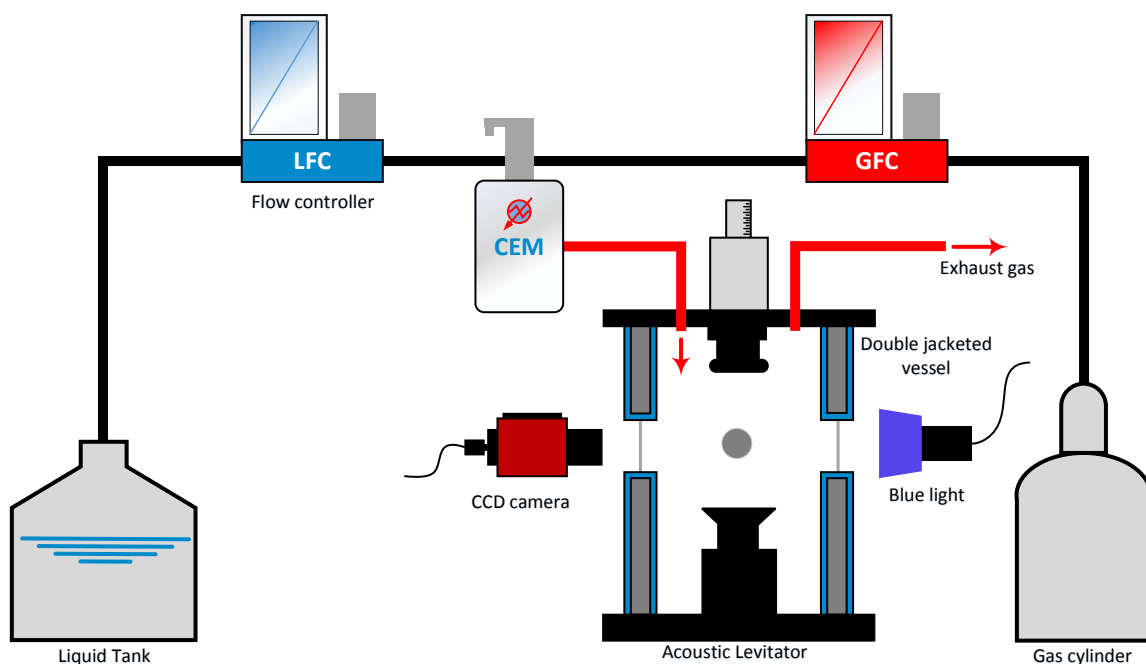


Figure 4: Scheme of the experimental apparatus used for single droplet drying. Briefly, it consists of a nitrogen gas cylinder, a liquid tank, liquid and gas flow controllers, a controlled evaporator mixer (CEM), temperature controlled chamber and an acoustic levitator which enables contactless droplet suspension. A light source and camera are used to observe the shrinking droplet.

### 328 5.3. *Data processing*

329 As evaporation of the droplet progresses in the chamber, the time evolution of the droplet diameter  
330 is monitored by analysing the projected area of the droplet obtained by optical imaging. The optical  
331 images obtained from the experiments are analysed by an automated image analysis routine using  
332 MATLAB. From this, droplet/particle properties such as projected area, axis lengths, centroid etc. are  
333 extracted. To account for droplet shape deformation caused by acoustic effects, a volume equivalent  
334 spherical diameter (estimated from the projected major and minor axis length of images) is extracted  
335 and used to describe the droplet/particle size. To guarantee compatibility of model and experimental  
336 results, values used to validate the model results are based on such equivalent spherical diameters and  
337 actual initial droplet diameters as obtained experimentally. Temperature and compositional changes  
338 within are not measured due to the lack of accurate spatially resolved techniques for the small droplet.

### 339 5.4. *Experimental Conditions*

340 To ensure the validity of experimental results, experimental drying conditions were calibrated using a  
341 temperature and humidity sensor (Thermochron DS1923 hydrochron Ibutton;  $\pm 1$  °C and  $\pm 2\%$  relative  
342 humidity) placed near the droplet in the levitation field. Typically, a 1.4  $\mu\text{L}$  droplet is levitated, giving  
343 a droplet diameter of  $\approx 1.4$  mm. Although obtaining exactly the same initial droplet size is difficult  
344 due to the manual handling of the syringe, deviations from the desired initial size are typically within  
345  $\pm 5\%$ . To test the ability of the model to capture a range of drying conditions, the effect of temperature  
346 and concentration is investigated for pure component and multicomponent systems. An overview of  
347 the experimental conditions is given in Table 1.

Table 1: Experimental conditions used for model validation - mass fractions are expressed on a solid-free basis

component(s)	temperature(s) [K]	$w_1$ (% w/w)	$w_2$ (% w/w)
water	313, 333, 343	100	0
Mannitol-water	333	1	99
	323, 333, 343, 353	4.5	95.5
	333	7.3	92.7
PVP-mannitol-water	333	4.8	4.5
	333	7.8	4.5
	333	15	4.5

## 349 6. Results and Discussion

350 The solution to the model equations given in Section 3 are implemented on MATLAB for several case  
351 studies, and are validated using experimental data as discussed in Section 5. To utilise the experimental  
352 data, drying conditions (gas temperature, humidity, velocity) must directly correlate with inputs to the  
353 model. The gas flow rate measured by the CEM (Figure 4) allows the inlet velocity to the drying  
354 chamber (for a given pipe diameter) to be determined. However, it is not possible to directly relate this  
355 velocity to the gas velocity experienced by the droplet in the drying chamber, but this is required for the  
356 calculation of the Reynold's number in Eq. (11). The velocity is obtained by treating it as a decision  
357 variable in an optimisation problem. Specifically, the  $\ell^2$ -norm of the difference between the simulated  
358 and experimental droplet diameter profile against time is minimised for the case of evaporating pure  
359 water at  $T = 333$  K and  $RH = 0\%$ . This results in a gas velocity of  $u_g = 0.095$  m s<sup>-1</sup> at a gas flow  
360 rate of 1 L min<sup>-1</sup>. Since this is a non-changing parameter for a given inlet flow rate, the value must  
361 be consistent with other systems evaporating under the same gas conditions. This was confirmed using  
362 the experimental data of several model systems (Table 1) under the same drying conditions where the  
363 model was used predictively.

Table 2: Table of parameters <sup>a</sup>.

parameter	value	parameter	value
$k_v$	0.02	$C_{p,\text{water}}$	4184 J kg <sup>-1</sup> K <sup>-1</sup>
A	$1 \times 10^{14}$ m <sup>-3</sup> s <sup>-1</sup>	$C_{p,\text{mannitol}}$	1312 J kg <sup>-1</sup> K <sup>-1</sup>
B	-3	$C_{p,\text{PVP}}$	2300 J kg <sup>-1</sup> K <sup>-1</sup>
$\rho_{\text{mannitol}}$	1520 kg m <sup>-3</sup>	RH	0%
$\rho_{\text{PVP}}$	1300 kg m <sup>-3</sup>	$u_g$	0.095 ms <sup>-1</sup>
$\rho_{\text{water}}$	1000 kg m <sup>-3</sup>	$h_c$	10 W m <sup>-2</sup> K <sup>-1</sup>
$\lambda_{\text{mannitol}}$	0.5 W m <sup>-1</sup> K <sup>-1</sup>	$\Delta H_{\text{crys}}$	$-3 \times 10^5$ J kg <sup>-1</sup>
$\lambda_{\text{PVP}}$	0.3 W m <sup>-1</sup> K <sup>-1</sup>	$k_g$	$2 \times 10^{-6}$ m s <sup>-1</sup>
$\lambda_{\text{water}}$	0.1 W m <sup>-1</sup> K <sup>-1</sup>	$\alpha$	1.2

<sup>a</sup> All the values shown here are assumed constant in the liquid phase. Temperature dependent properties used in the model are given as part of the supplementary information.

## 365 6.1. Non-particle forming systems

### 366 6.1.1. Evaporation of Pure component droplets

367 Firstly, the behaviour of the model is examined using the droplet drying history of pure component  
368 systems. The rate at which the radius of the droplet is decreasing is given by:

$$\frac{dr_s}{dt} = -\frac{\dot{m}_v}{4\pi r_s^2 \rho^{(C)}} \quad (22)$$

369 Godsave [42] and Spalding [43] showed that when the temperature of the droplet reaches the wet bulb  
370 temperature, usually after a rapid initial heating period, quasi-steady equilibrium is achieved and the  
371 well established  $d^2$  law (Eq. (23)) can be derived, assuming a gas-phase model i.e., negligible liquid  
372 phase heat and mass transfer (see supporting information for the derivation).

$$\frac{d(d^2)}{dt} = kt \quad (23)$$

373 where  $k$  is the evaporation constant. The above equation states that a plot of the droplet surface area  
 374 against time is linear for a pure component system. By normalising the droplet surface area at every  
 375 time with the initial surface area, it is indeed also more convenient to compare the drying history of  
 376 different droplets as experimentally observed. Figure 5 shows the evolution of the droplet diameter and  
 simulated temperature distribution for pure water. As expected for the case of pure water, the model

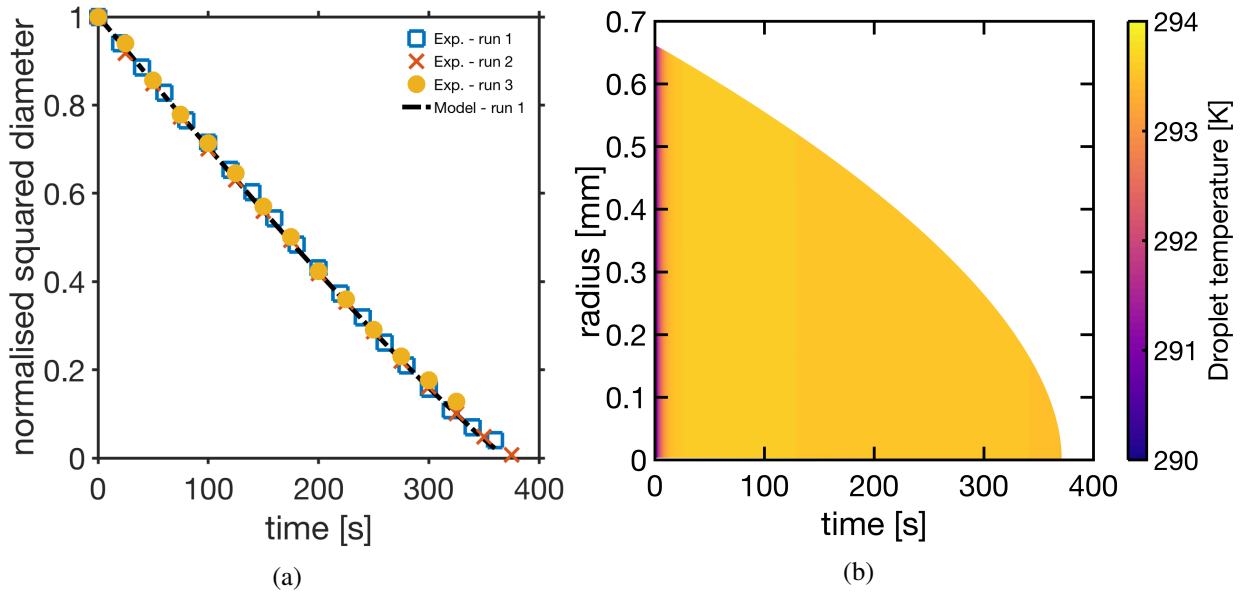


Figure 5: Evaporation of pure water at 333 K and 0 % relative gas saturation. Data points are recorded every second, but for display purposes fewer are shown. The value of some dimensionless numbers and parameters at the beginning of drying (290 K) and with a starting droplet diameter of 1.5 mm are:  $Re = 7.9$ ,  $Sc = 0.67$ ,  $Sh = 3.40$ ,  $\bar{Sh} = 3.39$ ,  $Le = 0.92$ ,  $Pr = 0.73$ ,  $B_M = 0.013$ ,  $B_T = 0.028$ . The time evolving profile of the Reynold and Sherwood numbers are further illustrated in Figure S1 of the supporting information. The value of the Biot number ( $Bi = 2h_{c,r_s}/\lambda$ ) obtained for a maximum heat transfer coefficient  $h_c$  of  $10 \text{ W m}^{-2} \text{ K}^{-1}$  is 0.03.

377

378 results show identical drying rates to that experimentally observed (results also show good repeatability  
 379 for 3 different runs). Although a slight deviation from the  $d^2$  law (Eq. (23)) is observed (i.e., the plot  
 380 of the normalised squared diameter against time is not a straight line, particularly towards the end of  
 381 the drying process). This can be rationalised by the relative motion between the droplet and the gas  
 382 phase. The Reynolds number is continuously decreasing during drying (cf. Figure S1 in the supporting  
 383 information). This change is in fact not accounted for in the derivation of the classical  $d^2$  law [44].  
 384 The evaporation model described here accounts for these effects. The results shown in Figure 5b fur-  
 385 ther illustrate the capability of the model to describe the evaporation phenomena down to very small  
 386 sizes ( $1 \mu\text{m}$ ); the physical sizing limit of the camera. This is based on the observation that the model  
 387 and experimental data are still in good agreement at these small sizes and therefore, this ability is in-

388 dependent from the initial size of the droplet. This is an important observation, because the initial  
 389 droplet size employed in the experiments (due to physical limitations) is much larger than those typi-  
 390 cally employed within spray drying operations. The temperature distribution in Figure 5b shows that  
 391 the temperature gradient within the droplet is negligible, which is a consequence of the small droplet  
 392 size and the high thermal conductivity of water. This can be further rationalised by the low Biot number  
 393 calculated ( $Bi = 0.03$ ; see the caption of Figure 5 for further characteristic dimensionless numbers).  
 394 Although the above results for water are based on values of optimised velocity experienced by the  
 395 droplet, by drying pure water droplets at different temperatures under the same drying gas condition,  
 396 one can determine the general applicability of the model. Figure 6 shows drying results obtained for  
 drying at different temperatures. The model results similarly show excellent prediction for drying at

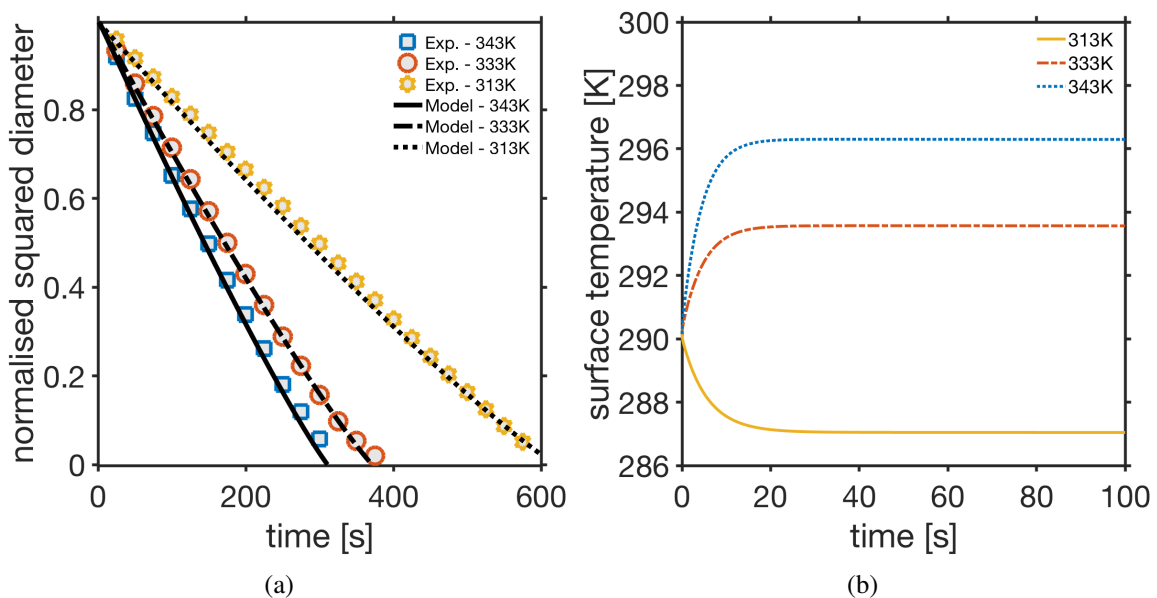


Figure 6: Effect of gas temperature on the evaporation of water at 0 % relative gas saturation. a) evolution of the normalised squared droplet diameter b) evolution of the surface temperature of the droplet.

397

398 different temperatures. As expected, the evaporation rate increases with an increase in temperature due  
 399 to a larger temperature driving force at constant relative saturation. In Figure 6, this is reflected by the  
 400 shorter drying time and the faster decrease in droplet diameter. As mentioned previously, the measure-  
 401 ment of droplet temperature is difficult experimentally with the resolution of applicable methods being  
 402 quite limited. Hence, surface temperatures obtained from the model here are compared to experimen-  
 403 tally observed wet bulb temperatures available from psychrometric charts [45, 46], see Table 3. The  
 404 predicted surface temperatures are also in good agreement with the experimentally observed wet bulb

405 temperatures reported in literature. The validity of the model is further substantiated in the supporting  
406 information where data for other pure components (methanol, ethanol, isopropanol) as well as binary  
407 mixtures of these solvents are shown.

408

409

Table 3: Comparison of experimental wet bulb temperatures and predicted surface temperatures<sup>a</sup>

component	gas temperature [K]	exp. wet bulb temperature [K]	model surface temperature [K]
water	313	287	287.0
water	333	293	293.6
water	343	295	296.3

<sup>a</sup> All simulations and experiments are at 0% relative saturation of the gas phase (N<sub>2</sub>).

## 410 6.2. Particle forming systems

411 In order to validate the model for systems forming particles within the droplet, a homogeneous aqueous  
412 solution of mannitol and a ternary solution containing mannitol and PVP is considered. The activity of  
413 components in all solutions are determined using the UNIFAC group contribution method as discussed  
414 in Section 3.1.5. Details of the UNIFAC model are provided in the supporting documentation.

### 415 6.2.1. D-Mannitol in water

416 In the drying of a homogeneous solution containing mannitol and water, the initial droplet is a clear  
417 undersaturated solution (starting concentration, 7.3% w/w solution), with the solute and temperature  
418 distribution assumed to be uniform initially within the droplet. The temperature dependence of the  
419 binary diffusion coefficient in solution is modelled using the Stokes-Einstein equation [29]. Due to the  
420 formation of solid particles within the droplet, an effective diffusivity must be considered to account for  
421 the effect of the evolving solid particles on drying. The effective diffusivity  $D_{\text{eff}}$ , which is a combination  
422 of both surface diffusion and pore diffusion is accounted for using the Clausius-Massotti model [47].  
423 Since D-mannitol adsorbs water very weakly [48], one can assume that surface diffusion is negligible.

424 This simplifies the Clausius-Massotti model to Eq. (24):

$$D_{\text{eff}} = \frac{2D(1 - 2\varepsilon)}{2 + \varepsilon} \quad (24)$$

425 where  $D$  is the pore diffusion coefficient (derived from Stokes-Einstein equation). This diffusion coef-  
426 ficient is used in all relevant conservation equations. The nucleation and growth kinetics of D-mannitol  
427 are based on the empirical functional forms Eq. (7) and Eq. (8). The kinetic constants used for the  
428 simulation here is shown in Table 2 and are that obtained from Cornel et al. [49], except the value of  $A$   
429 which represents the maximum nucleation rate. As a result of the complexity of nucleation processes,  
430 the value of the maximum nucleation rate can vary between similar systems and process scales. In the  
431 present model application, this parameter is obtained by monitoring the time at which shell formation  
432 is observed. This analysis gives a reasonable nucleation rate of  $A = 1 \times 10^{14} \text{ m}^{-3} \text{ s}^{-1}$  [49]<sup>1</sup>. The  
433 results obtained from the simulation for the droplet diameter profile is shown in Figure 7 and an ex-  
434 cellent prediction is made up to the critical point. The concentration profile of mannitol illustrates that  
435 as the solution droplet dries, a concentration gradient is built up within the droplet over time with the  
436 highest concentration of solute at the droplet surface (Figure 8a). The concentration increases due to a  
437 reduction in droplet size as a result of evaporation. After the saturation point of the solute in the solvent  
438 is reached, continuous evaporation and droplet shrinkage causes the concentration to exceed the satu-  
439 ration concentration, providing a driving force in terms of supersaturation for crystallisation. The solid  
440 fraction (Figure 8b) increases very quickly towards the end of drying due to the exponential increase  
441 in nucleation rate (Eq. (7)) with supersaturation. This is complemented by a much larger number of  
442 crystals growing towards the end of the first drying stage. Shell formation (critical point) is predicted  
443 at a solid fraction of 0.32, at  $\approx 266$  s and final droplet diameter of 0.8 mm, which matches the experi-  
444 mental observation well (Figure 7; 270 s experimentally). When drying is allowed to continue until a  
445 solid fraction of 0.7, shell formation occurs at 271 s, with a final droplet diameter of 0.76. This shows  
446 that the effect of PSD on the critical point may not be significant for the model system considered here.  
447 At the critical point, the shell can lock due to the presence of electrostatic interaction between particles

---

<sup>1</sup>While this value is different from the one reported in Cornel et al. [49] for the  $\alpha$  polymorph, it is important to remember that the original authors did not quantitatively estimate these values from experimental data, but merely have used it to reconstruct the qualitative behaviours seen in their data.

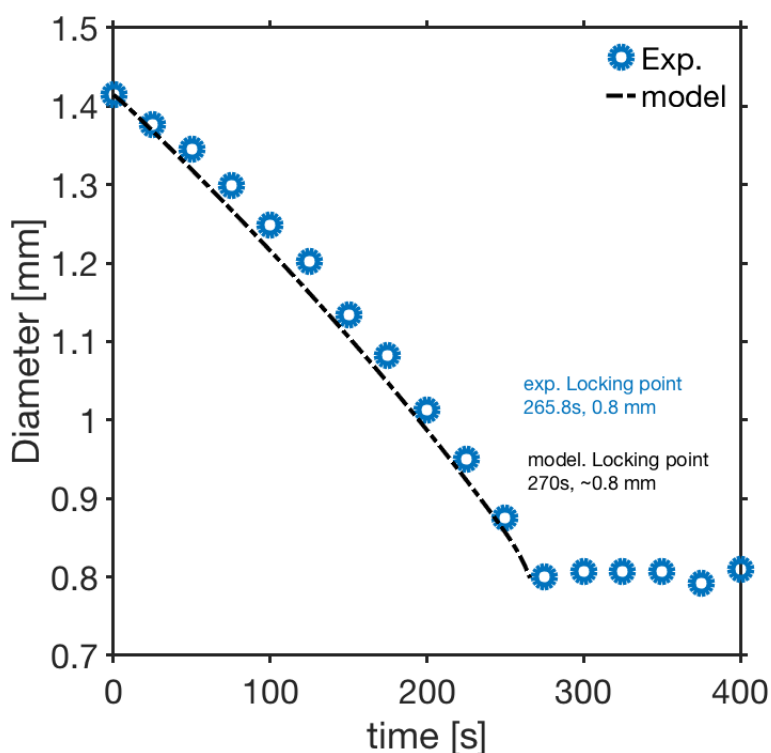


Figure 7: Model and experimental results for the drying history of a droplet containing an aqueous solution of D-mannitol (7.3% w/w D-mannitol) at 333 K and 0% relative gas saturation.

448 at the particle-dense surface. However, this must be balanced by the ability of the shell to withstand  
 449 surrounding pressures (external and capillary pressures) [20, 50]. When a strong shell is not formed  
 450 instantaneously, there may exist a droplet-particle transition regime (shell thickening regime) where  
 451 the pressures exerted on the forming shell causes a cycle of shell buckling events until the shell is ca-  
 452 pable of withstanding the stress forces acting on the droplet/particle surface [50]. As such, the droplet  
 453 may still continue to shrink, albeit more slowly due to the high resistance to evaporation at the particle  
 454 dense surface. Nevertheless, the results shown here for this model system do not show this behaviour  
 455 (as seen from the constant particle diameter after the critical point; cf. Figure 7). This highlights that  
 456 the model devised here is applicable to this model system. As expected from the temperature profile of  
 457 the droplet (Figure 9), the droplet temperature rises to the wet bulb temperature of the solution. Since  
 458 the concentration of the solution is not constant, the wet bulb temperature varies slightly over time  
 459 and will depend on the evolving physical properties of the liquid mixture. Near the critical moisture  
 460 content, the temperature begins to rise to the gas temperature (cf. Figure 1) when drying below the  
 461 boiling point. Figure 10 shows an example particle size distribution (PSD) during drying. This figure

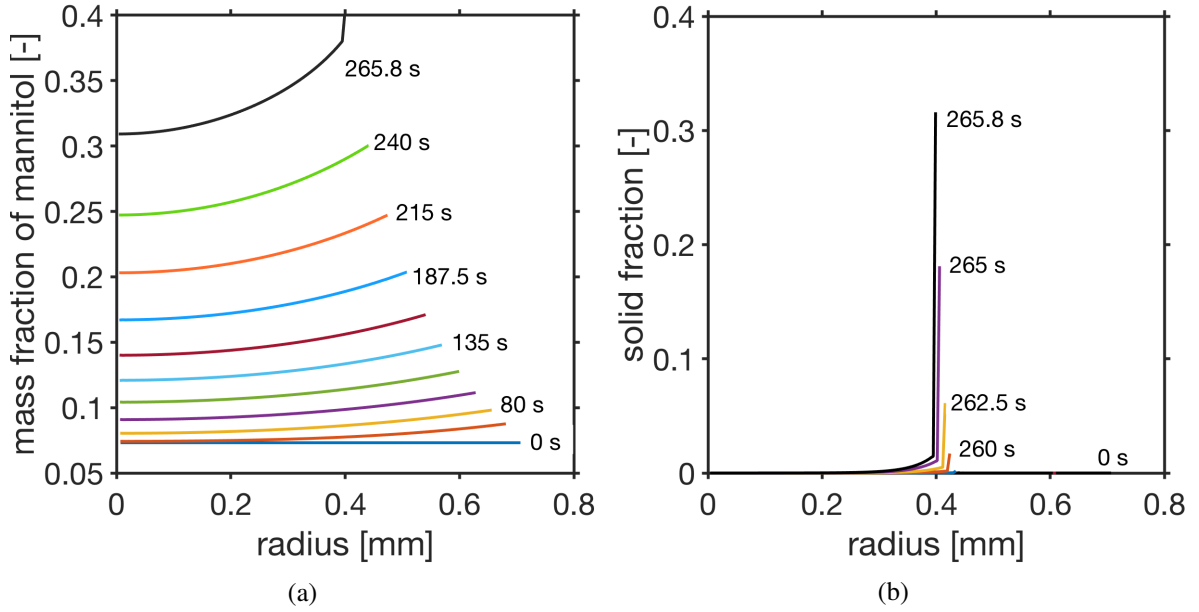


Figure 8: simulated results for the a) concentration and b) solid fraction profile of a droplet containing an aqueous solution of D-mannitol (7.3% w/w D-mannitol) drying at 333 K and 0% relative gas saturation.

462 represents the PSD present at all radial coordinate points at 240 s. Therefore, a horizontal line in this  
 463 figure represents the PSD at a specific radial location, with the value of the PSD shown with a colour  
 464 scale (see colour bar on the right; note the logarithmic scale). The PSD at the liquid/gas interface ( $r$   
 465  $\approx 0.42$  mm) shows both the largest particles and the highest number of particles. This is due to the  
 466 supersaturation at the interface being the highest throughout the drying process, which results in high  
 467 nucleation and growth rates (cf. Eq. (7) and Eq. (8)). To allow a more quantitative evaluation a series  
 468 of time evolving profiles of reduced properties of the PSD will be shown. Specifically, the integrals of  
 469 the PSD along the  $L$  and  $r$  direction is introduced:

$$N_{i,L}(t, r) = \int_0^{\infty} N_i(t, r, L) dL \quad (25)$$

$$N_{i,r}(t, L) = 4\pi \int_0^{r_s} r^2 N_i(t, r, L) dr$$

470 The first property,  $N_{i,L}$ , therefore represents the total number of particles (of any size) at a specific  
 471 radial coordinate  $r$  and time  $t$ . The second property,  $N_{i,r}$  represents the number of particles of size  $L$  per  
 472 droplet volume at a specific time  $t$ . Profiles of these properties at specific times are shown in Figure 11.

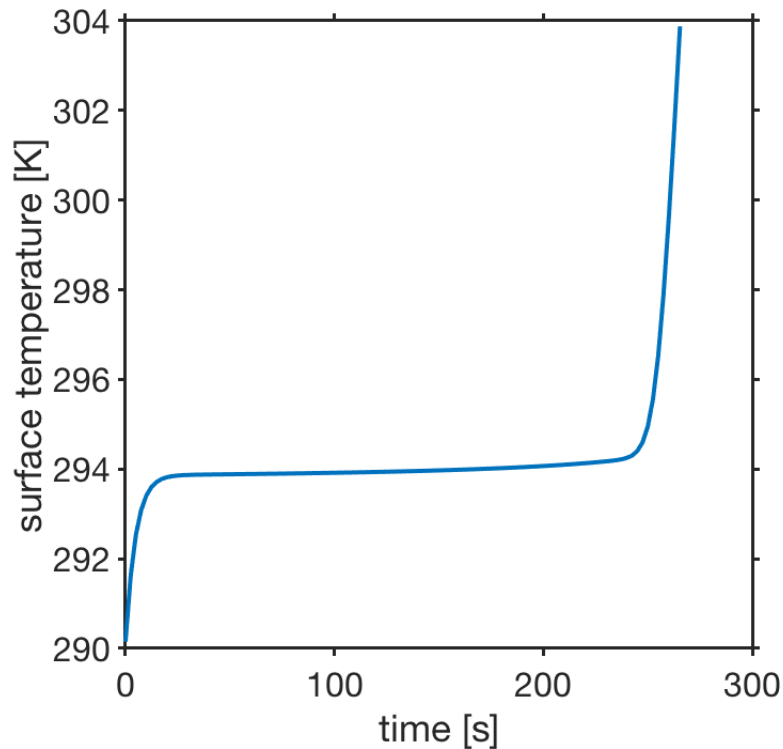


Figure 9: simulated temperature profile of 7.3% w/w aqueous mannitol solution droplet drying at 333 K and 0% relative gas saturation.

473 Figure 11a illustrates the time evolution of  $N_{i,r}$ , where the total PSD within the droplet (acting as if  
 474 it is well mixed) is shown. At the beginning of drying, there are no particles and as drying proceeds  
 475 and the solution becomes supersaturated, nucleation occurs at small sizes and growth of crystals is  
 476 observed in the droplet. It can also be observed that a smaller number of larger crystals exists within  
 477 the droplet when compared to the number of smaller crystals present. This results from the fact that  
 478 the supersaturation achieved within the droplet becomes much higher as the droplet becomes smaller.  
 479 Just prior to shell formation (260 - 265s in Figure 8b), the supersaturation is consumed significantly  
 480 that the number of nuclei formed within the droplet begins to decrease again (seen as a dip of  $N_{i,r}$  at  
 481 small sizes). The results also show that particles up to 100  $\mu\text{m}$  can be produced within the droplet. An  
 482 exemplary scanning electron microscopy (SEM) image of the final particle obtained (Figure 12) shows  
 483 that this is indeed very possible. Figure 11b shows the evolution of  $N_{i,L}(t, L)$ , with the concentration of  
 484 particles highest at the droplet surface. Due to advection and diffusion, a significant amount of particles  
 485 are also formed at the centre of the droplet.

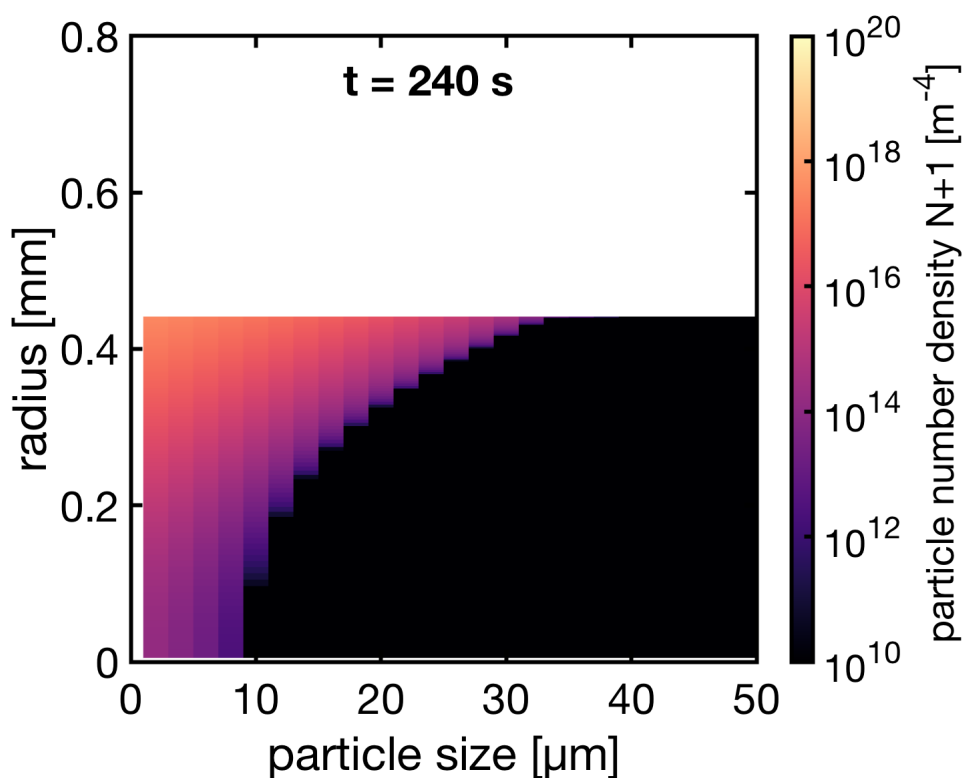


Figure 10: Simulated particle size distribution (PSD) of mannitol at 240 s.

486 In order to further test the predictability of the model, droplets drying at different gas temperatures  
 487 and starting concentrations are investigated. The predicted drying profile of the droplets is shown in  
 488 Figure 13. These profiles indicate an excellent predictability of the drying history for the range of  
 489 conditions considered. The key results obtained are summarised in Table 4. As the concentration of  
 490 mannitol increases from 0.9% w/w to 11.2% w/w, the time of shell formation reduces owing to the faster  
 491 and higher solute enrichment at the droplet boundary. This leads to faster particle formation kinetics  
 492 and hence, droplets with high initial solute concentration will produce particles with larger sizes, as  
 493 opposed to droplets with a lower starting concentration. In the case of drying at different temperatures,  
 494 a good prediction is also made <sup>2</sup>, with the time of shell formation seen to decrease due to the higher  
 495 evaporation rates. However, a significant trend is not observed for the final particle diameter. This  
 496 shows that the competition between the convective process and particle formation may be significant

<sup>2</sup>The result presented for the different temperatures here assumes that the particle formation kinetics do not change with temperature. In reality, the nucleation and growth rate of particles increases with temperature. The predicted result however still shows good comparisons with experiment.

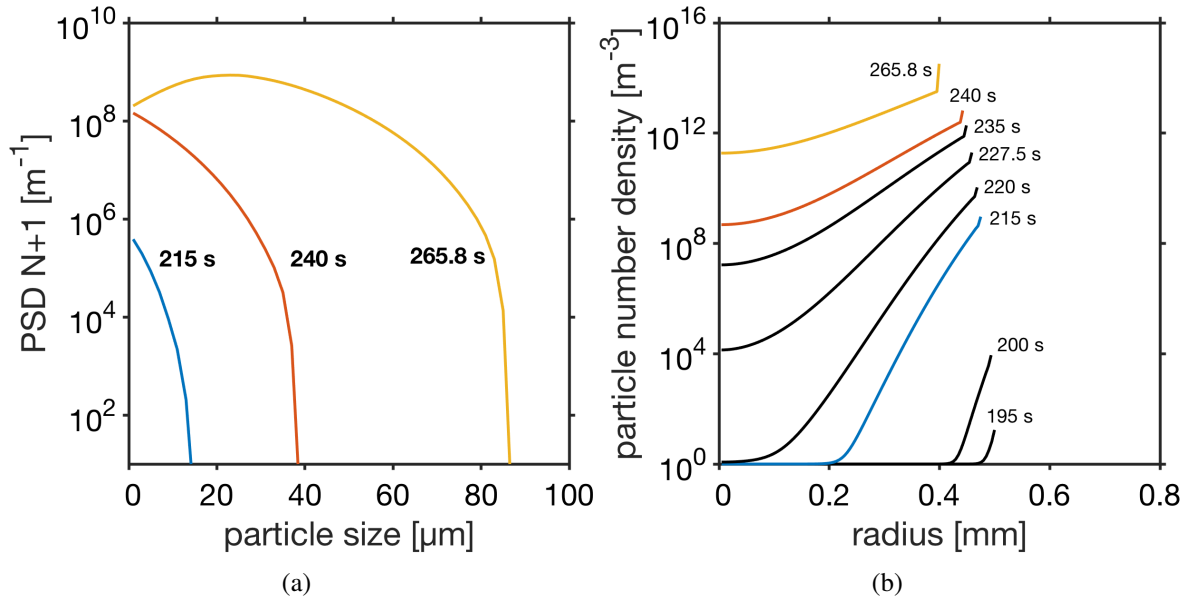


Figure 11: a) evolution of the total particle number density in the droplet, assuming a well mixed droplet b) evolution of the total particle number density at each radial location during the drying of a droplet of 7.3% w/w aqueous mannitol solution at 333 K and 0% relative gas saturation.

497 when drying particle forming formulations. Analysis of the Peclet number  $Pe = \frac{k}{8D}$  shows that the  
 498 Peclet number decreases, although not significantly as the starting concentration of solute is increased  
 499 (Table 4). Again, no trend is particularly observed in the case of varying drying temperatures. Overall,  
 500 the results indicate that the model is able to predict droplet size and the time of shell formation with  
 501 good accuracy for a large range of initial concentrations and for the range of temperatures considered.

502

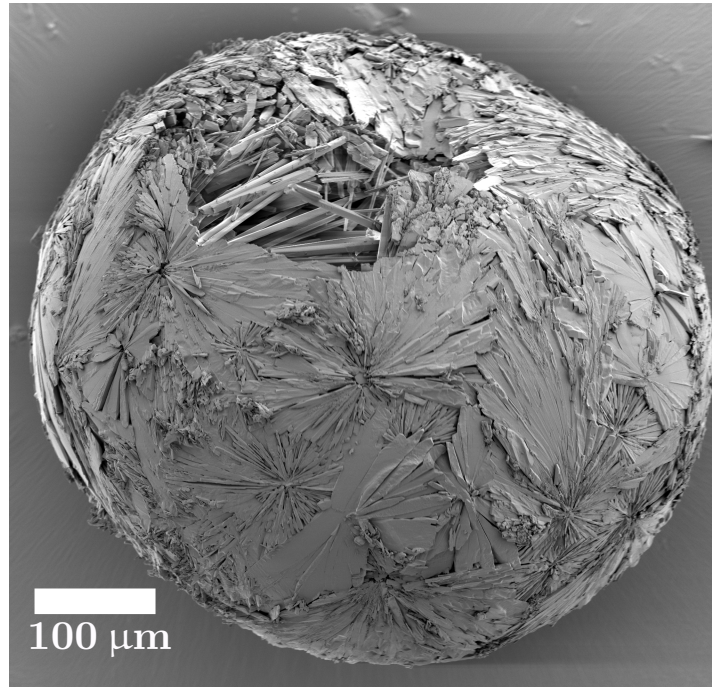


Figure 12: SEM image of a mannitol particle manufactured from a droplet with initial concentration of 4.5% w/w mannitol in water, and dried at 313 K and 0% relative saturation. The final particle structure supports the crystallization model used, and also shows that crystal sizes larger than 100  $\mu\text{m}$  can be obtained as illustrated in Figure 11.

503

Table 4: Experimental and model results for the drying of mannitol solutions for different initial droplet concentrations and temperature <sup>a</sup>.

Initial mannitol concentration $w_{\text{initial}}$ (% w/w)	0.9	4.5	4.5	4.5	4.5	7.3	11.2
Initial droplet diameter [mm]	1.41	1.24	1.36	1.36	1.27	1.41	1.31
Drying temperature [K]	333	323	333	343	353	333	333
Evaporation constant $k$ [ $\times 10^{-9} \text{ m}^2 \text{ s}^{-1}$ ]	4.96	3.90	5.18	5.89	6.23	5.24	5.18
Peclet number [-]	0.95	0.75	0.94	0.96	0.94	0.92	0.87
Final experimental droplet diameter [mm]	0.37	0.57	0.63	0.61	0.63	0.81	0.86
Final predicted droplet diameter [mm]	0.36	0.59	0.63	0.62	0.56	0.78	0.86
Experimental critical point [s]	380	315	280	255	195	270	190
Predicted critical point [s]	381	291	290	245	195	266	189

<sup>a</sup> All simulation and experimental data shown are obtained at 0% relative saturation of the gas phase ( $\text{N}_2$ ) and a gas velocity of  $0.095 \text{ m s}^{-1}$ . The Peclet number is calculated using an average  $k$  value i.e., average of the  $k$  values obtained at every time step and the diffusion coefficient is calculated using the starting droplet concentration.

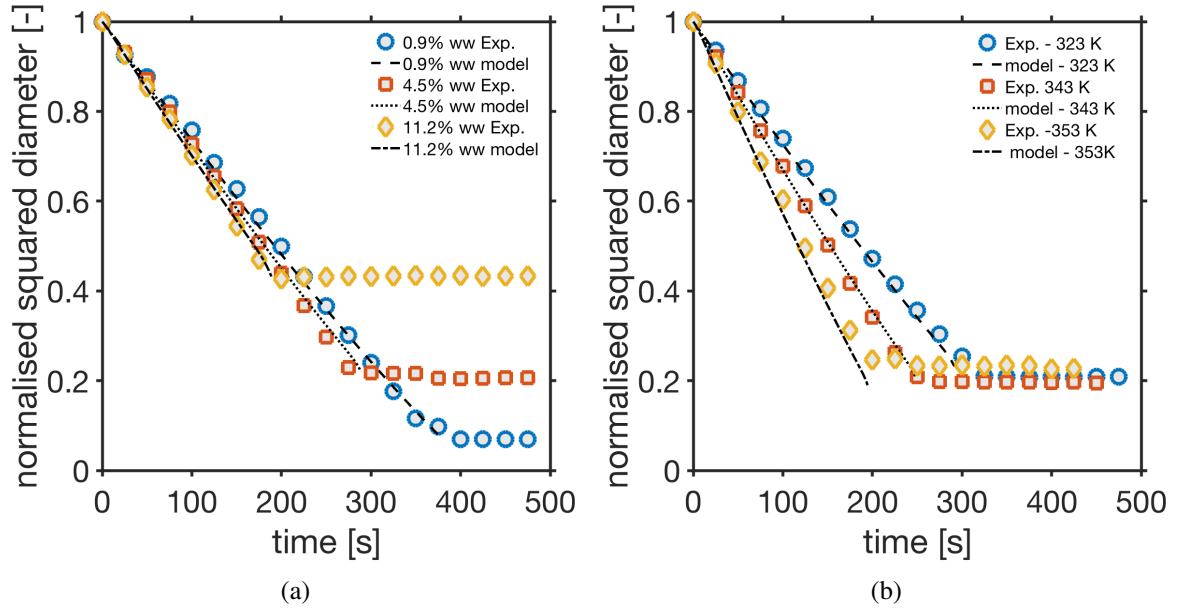


Figure 13: Droplet drying history of mannitol at a) different concentrations and b) different temperatures.

#### 504 6.2.2. PVP and D-Mannitol in water

505 The evaporation of a ternary system containing PVP and D-mannitol in water is now considered.  
 506 Since experimental data for diffusion for multicomponent systems are often unavailable, multicomponent  
 507 diffusivity must be predicted instead. Cussler [29] showed that the well established relations  
 508 for Maxwell-Stefan diffusion coefficients can be related to Fick's diffusion coefficient using thermo-  
 509 dynamic relations. In this work, such complexity is streamlined for a more simplistic, but physically  
 510 reasonable approach. The diffusive fluxes of the solutes in such solute-solute-solvent systems can be  
 511 treated independently (assuming the cross diffusion coefficients are small) to yield estimates of diffu-  
 512 sivity [51]. By assuming the fluxes are relative (i.e. the total volume flux of solutes is equal to the  
 513 solvent flux) and combining this with the ratio of the diffusive flux of the two solutes i.e.,  $s = \frac{D_{13} \frac{\partial c_1}{\partial t}}{D_{23} \frac{\partial c_2}{\partial t}}$ ,  
 514 one can relate the independent solute diffusivity to the diffusivity of the solvent to give the expressions  
 515 [51];

$$D_1 = s \frac{\rho_1 \rho_2}{\rho_3 (\rho_2 s + \rho_1)} D \quad (26a)$$

516

$$D_2 = \frac{\rho_1 \rho_2}{\rho_3 (\rho_2 s + \rho_1)} D \quad (26b)$$

517 where the subscript 1,2,3 denote the D-mannitol, PVP and water, respectively and  $D$  is the binary dif-  
518 fusivity of the dominant solute (depending on the starting concentrations). To describe the non-ideality  
519 of the solution, the standard UNIFAC procedure combined with a free volume parameter estimation  
520 [27] is used. The change in solubility of mannitol in the mixture is assumed to be negligible i.e., the  
521 solubility is the same as in water. This assumption may affect the degree of supersaturation reached  
522 within the droplet and hence the extent of nucleation and growth of particles at any given time. This  
523 effect is however expected to be reduced since the higher viscosity of polymer mixtures also lead to  
524 a reduction in the kinetics of particle formation. The binary diffusion coefficient of PVP in aqueous  
525 solutions is estimated from experimental data [52]. As discussed in Section 6.2.1, mannitol solidifies  
526 to form crystals. The phase behaviour of PVP can be described by its viscosity profile (Figure 14a),  
527 where the viscosity increases exponentially with concentration. This results from the cross-linking of  
528 the long-chain polymer in the solvent. At a sufficiently high concentration, the degree of cross-linking  
529 is high so that the polymer forms a stable 3-dimensional solid-like structure - a gel. During the first  
530 drying stage, the polymer will act to inhibit the kinetics of crystal formation of mannitol due to the con-  
531 tinuously changing solution properties, specifically by altering the solution viscosity and, potentially,  
532 the interfacial tension between the liquid and solid; both of which affect the kinetics of nucleation  
533 and growth. Increasing the viscosity decreases the rate constants of nucleation and growth,  $A$  and  $k_g$   
534 [53, 54]. Increasing interfacial tension increases the thermodynamic parameter of the nucleation rate  
535 [53]. However, Bolten and Türk [55] showed that the surface tension of PVP/water solutions is nearly  
536 constant over a wide range of concentrations, thus the parameter  $B$  is kept unchanged.  $A$  and  $k_g$  on the  
537 other hand are adjusted by multiplying them with the ratio of the viscosity of water to the polymer so-  
538 lution [53]. The gelation of PVP in a binary solution of PVP and water is predicted from experimental  
539 viscosity data [56], where the viscosity increases exponentially with PVP concentration. The value of  
540 the gelation fraction is taken as 50% w/w concentration (Figure 14a) i.e., the point where the viscosity  
541 of the solution increases sharply. The simulation of the drying history of the binary mixture of PVP and  
542 water is shown in Figure 14b and compares well with experimental results. When the drying history  
543 of the droplet for the binary solution of PVP-water (Figure 14b) and mannitol-water (Figure 8) is com-  
544 pared, the formation of a shell occurs at similar times. In the ternary solution of PVP-mannitol-water,  
545 defining a critical point is more complex due to the functional relationship between the solutes, crystals  
546 and the gelation property of the polymer. The critical point in such a ternary solution is neither the

547 gelation point of the pure polymer nor the critical solid fraction of the evolving crystals. Instead, it is a  
 548 value that is expected to be below the critical values of the binary solutions. The critical point can in-  
 549 stead be empirically observed from the fact that the droplet surface temperature rises at some point due  
 550 to the increased resistance to evaporation caused by the accumulation of solutes/particles at the surface  
 551 (this is represented as point C in Figure 1). Note that in the binary case of mannitol-water (cf. Figure 9),  
 552 the temperature rise is also observed near the point of shell formation. In the present application on a  
 553 ternary system, a critical temperature is defined as an indication of shell formation. A value of 300 K  
 554 ( $\approx 2.5\%$  higher than the wet bulb temperature ( $\approx 293$  K) observed during most of the first drying stage  
 555 Figure 9) is used, and therefore shell formation will occur when the surface temperature of the droplet  
 556 reaches the predefined critical temperature. While this value is somewhat arbitrary, the methodology  
 of relating the critical point to the temperature rise is physically sound (cf. Section 2). Figure 15 shows

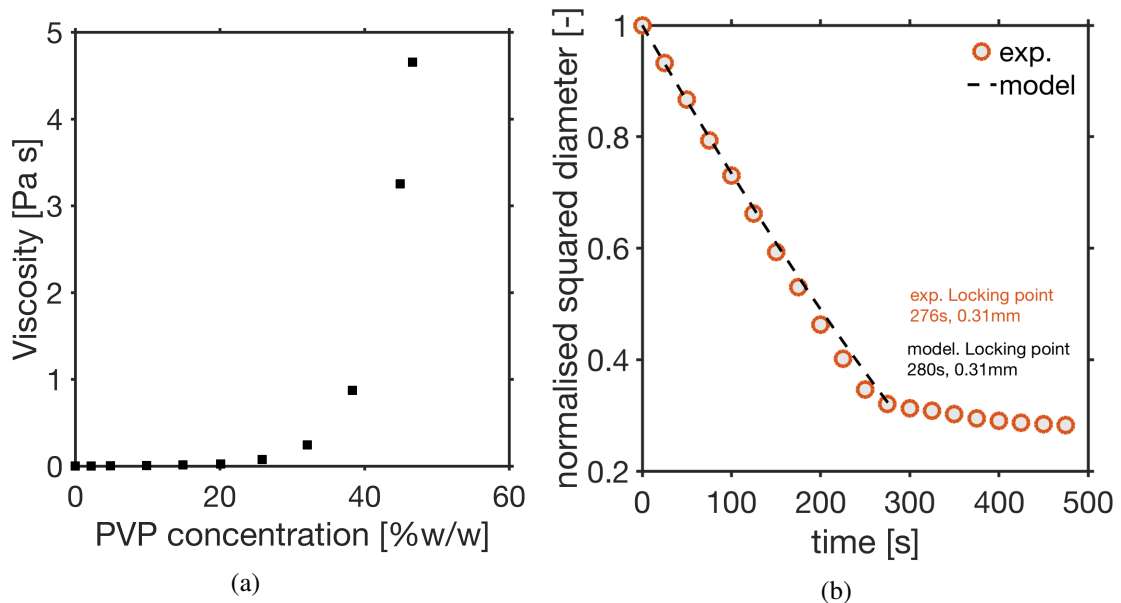


Figure 14: a) Viscosity data of PVP in aqueous solutions adapted from Ashland [56], b) drying behaviour of a droplet of aqueous solution of PVP (6% w/w) at 333 K and 0% relative gas saturation.

557

558 the evolution of the droplet diameter for PVP-mannitol-water solution (4.8% w/w PVP, 4.5% w/w man-  
 559 nitol). The model also predicts the drying history well in this case. In this plot, a comparison of the  
 560 methodology of shell formation at a critical temperature is compared to a case where the temperature is  
 561 allowed to rise until it reaches the gas temperature (when drying below the boiling point). In the latter  
 562 case, there is a deviation from the experimentally observed profile. This behaviour is not surprising

563 since shell formation is expected to precede a shell thickening regime. When a critical temperature is  
 564 not defined as above, the added resistance to moisture caused by the formation of a jammed shell layer  
 565 in the thickening regime is not accounted for c.f. Section 6.2.1 [19]. It is indeed clear from Figure 15  
 566 that a shell thickening regime exist since a sharp transition from droplet drying to particle drying is not  
 observed as in the case of drying aqueous mannitol droplet (Figure 7). Figure 16 shows the evolution

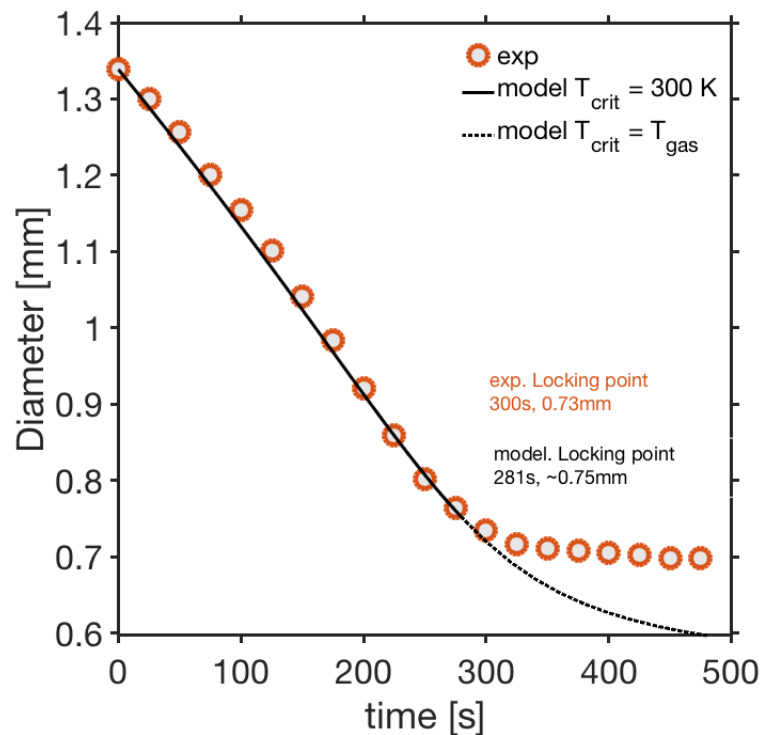


Figure 15: The drying history of a droplet containing an aqueous solution of PVP and D-mannitol 4.8% w/w PVP, 4.5% w/w mannitol and drying at 333 K. The solid line (-) shows the drying profile and critical point when a critical temperature is predefined, while the dotted line (..) shows the profile when drying is allowed to continue until the surface temperature reaches the gas temperature.

567

568 of the liquid phase mass fractions. The result indicates a high mass fraction of mannitol at the droplet  
 569 surface. This can be rationalised to be the effect of the reduced diffusion rate of the solute molecules  
 570 resulting from the increased solution viscosity (i.e.  $D \propto \frac{1}{\eta}$ ). Nevertheless, the mass fraction of both  
 571 solutes are seen to be highest at the droplet surface at all times, as expected. The droplet shows a similar  
 572 temperature profile to the binary system Figure 9. Figure 17a further shows the drying histories ob-  
 573 tained for different starting concentrations of PVP, while Figure 17b shows the corresponding relative  
 574 concentration of the components at the surface. Similar to the binary system, shorter drying times and  
 575 larger particle sizes are obtained with increasing PVP concentration. Figure 18 shows the evolution of

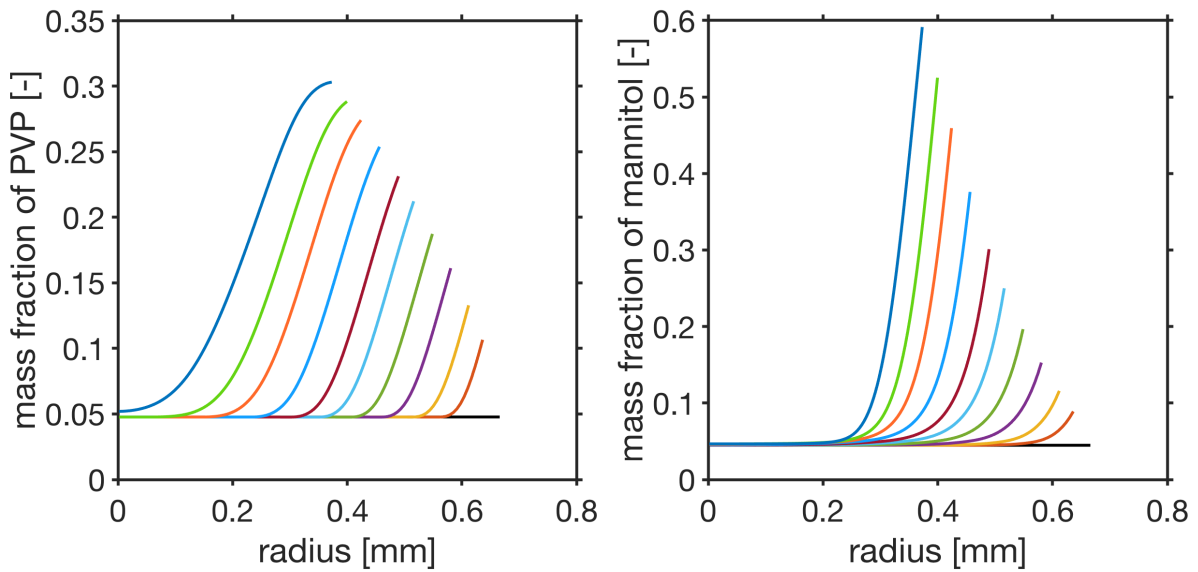


Figure 16: Model and experimental results for the drying of a droplet containing an aqueous solution of PVP and D-mannitol, 4.8%w/w PVP, 4.5%w/w mannitol, 333 K. This shows the mass fraction of mannitol in the liquid (left) and the mass fraction of PVP in the liquid (right).

576 the total number of mannitol particles within the drying droplet. As expected, this follows a similar  
 577 profile to the case of mannitol-water solution (Figure 11) albeit the total number of particles is much  
 578 lower than that of the binary case due to the reduced kinetics resulting from the increasing solution  
 579 viscosity. This is further illustrated by the reduced solid fraction (Figure 19) at the droplet surface at  
 580 the time of shell formation, indicating the dominating effect of the polymer gelation. Note that in this  
 581 figure, the high mass fraction of mannitol seen will decrease significantly as drying proceeds following  
 582 shell formation and the density of mannitol particles increases. The final polymer concentration at the  
 583 point of shell formation is  $\sim 35\%$  w/w, a value lower than that of the binary PVP-water system. As  
 584 discussed previously, this highlights that the critical point for the ternary system considered here is  
 585 not equivalent to either critical points of the binary systems (i.e. PVP-water and mannitol-water). The  
 586 SEM image shown in Figure 20 further supports this claim, as the shell is visually observed to consist  
 587 of crystals, while the number of crystals is significantly reduced when compared to the binary system  
 588 Figure 12.

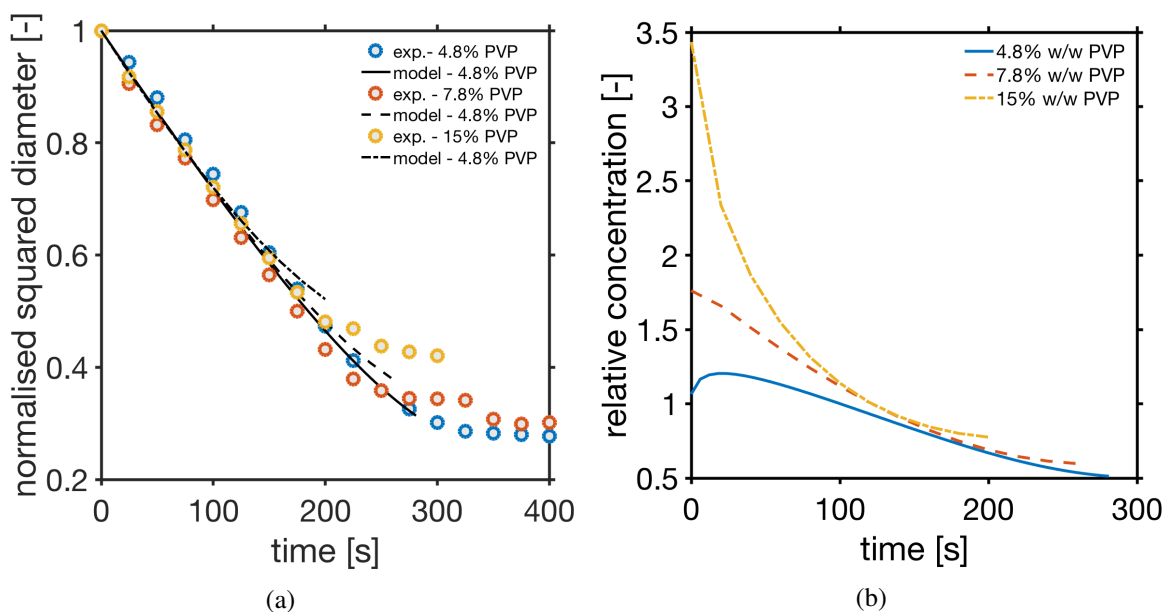


Figure 17: Application of the model to droplets with different starting PVP concentrations in 4.5% w/w mannitol and drying at 333 K a) evolution of the droplet diameter b) evolution of the relative concentration of PVP to mannitol at the surface of the droplet.

## 589 7. Conclusion

590 A model consisting of mass, energy and population balance equations was developed for the drying  
 591 of solution droplets. The drying history of the droplet until the point of shell formation was described  
 592 through the coupling of mass balances over the liquid phase, the solid phase and internal/external en-  
 593 ergy transport. By considering case studies involving water, we show that the current model provides  
 594 a sophisticated description of the history of droplets drying in a controlled environment. As illustrated  
 595 from the model case studies, such a mechanistic description can be adapted to glass forming formu-  
 596 lations (amorphous systems) if diffusion coefficients can be estimated within an acceptable level of  
 597 accuracy. The use of UNIFAC group contribution method to describe the non-ideality of the liquid  
 598 phase in mannitol and PVP-mannitol solutions is shown to be appropriate for the cases considered.  
 599 Nevertheless, for other mixtures different activity coefficient models might be necessary. The simula-  
 600 tion of droplet temperature profile shows that the temperature is near-uniform at all times during the  
 601 first drying stage, and agrees well with available literature values of wet bulb temperatures. However,  
 602 for the second drying stage temperature gradients are likely to be more pronounced, so that from a  
 603 perspective of model consistency, considering the gradients already in the first drying stage is prudent.

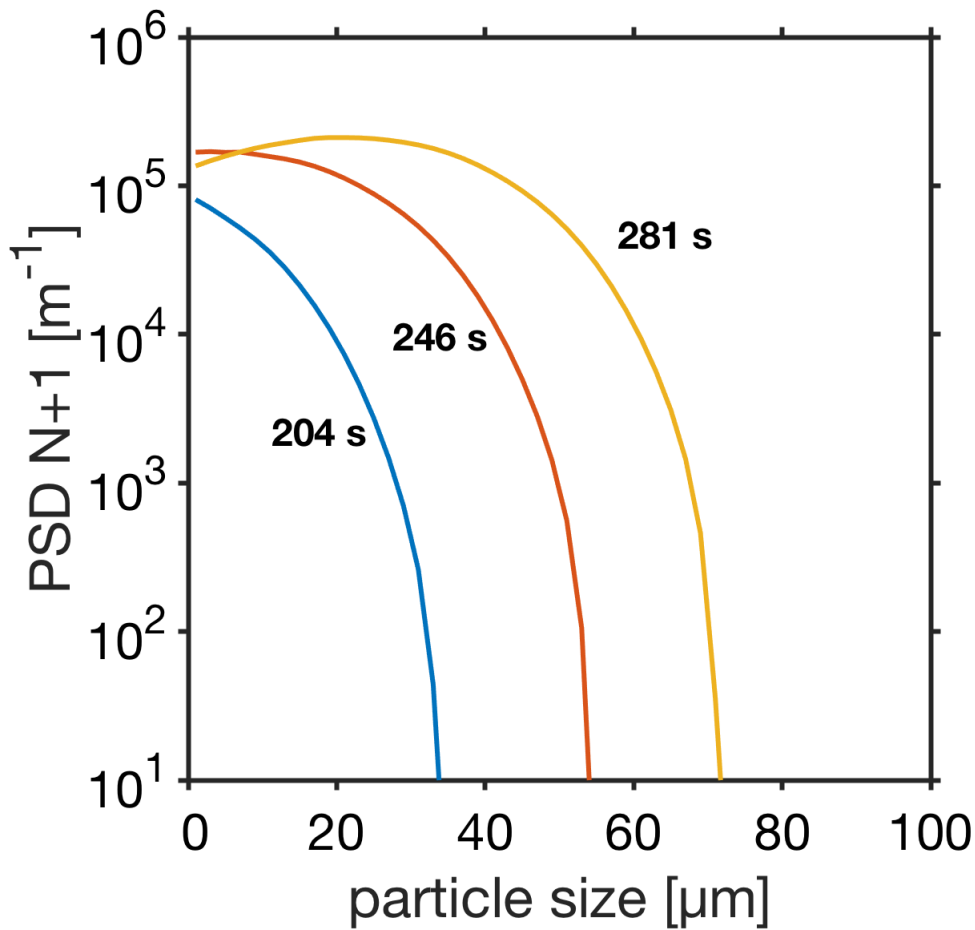


Figure 18: The evolution of the total number density of particles in the droplet during the drying of an aqueous solution of PVP and mannitol; 4.8% w/w PVP, 4.5% w/w mannitol at 333 K.

604 The time of shell formation and diameter for mannitol and PVP-mannitol solutions are predicted within  
 605 an acceptable margin of error. In the case of a mannitol solution, the effect of the initial droplet con-  
 606 centration and temperature was investigated . The results show that as the concentration is increased  
 607 from approximately 1% w/w to 11% w/w, the drying times become shorter and larger particles sizes  
 608 are obtained, as expected. Similarly, increasing the temperature led to shorter drying times however,  
 609 no significant trend was observed for the particle size. The model when applied to a more complex  
 610 formulation involving a crystalline solute, polymer and a solvent shows excellent predictability and  
 611 further demonstrates the capability to describe the drying behaviour of such mixtures as well. Whilst  
 612 the mechanistic description of transport within a droplet shown here represents a step towards predict-  
 613 ing particle morphologies, the drying process following shell formation needs to be further described  
 614 for that to be possible. This work represents a vital contribution towards being able to predict particle

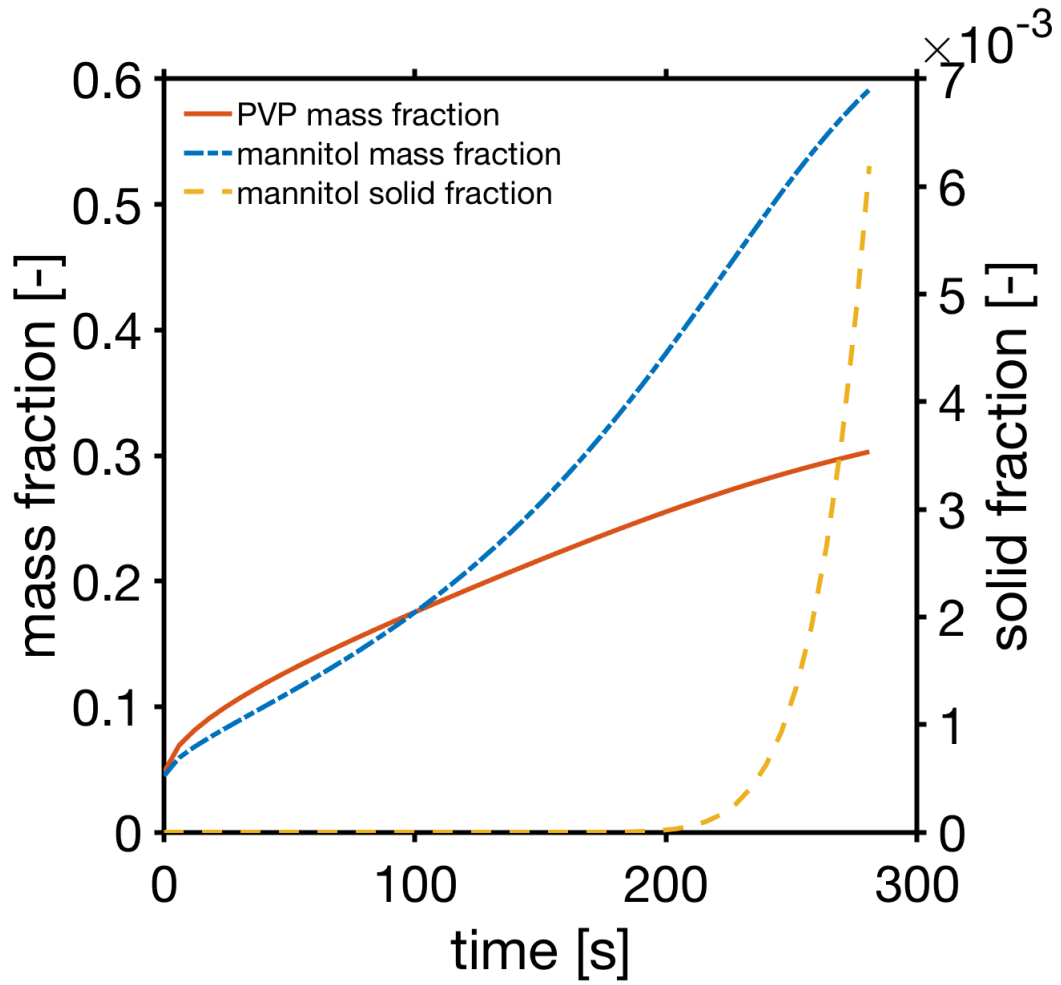


Figure 19: evolution of solute mass fractions and the solid fraction of mannitol at the droplet surface during the drying of a droplet containing an aqueous solution of PVP and mannitol; 4.8% w/w PVP, 4.5% w/w mannitol at 333 K.

615 morphologies and the PSD obtained also has great potential for pharmaceutical delivery applications.

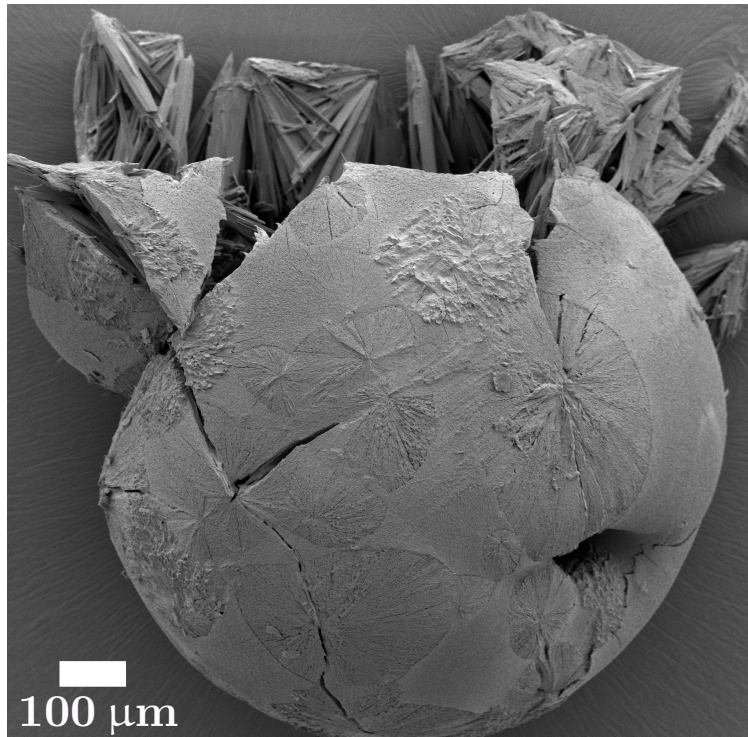


Figure 20: SEM image of a particle manufactured from a droplet with initial concentration of 4.8% w/w PVP in 4.5% w/w mannitol in water, and dried at 313 K and 0% relative saturation. The number of crystals formed within is observed to decrease significantly in the presence of PVP when compared to the case of mannitol-water shown in Figure 12.

616 **Acknowledgments**

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618 **Abbreviations**

619 **API** active pharmaceutical ingredient

620 **CEM** controlled evaporator mixer

621 **LFC** liquid flow controller

622 **GFC** gas flow controller

623 **PBE** population balance equations

624 **PSD** particle size distribution

625 **PVP** polyvinylpyrrolidone

626 **SDD** single droplet drying

627 **UNIFAC** UNIQUAC functional group activity coefficients

628

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