

1 Separation Of Conglomerate Forming Enantiomers
2 Using A Novel Continuous Preferential
3 Crystallization Process

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10 **Abstract**

11 Providing enantiomerically pure products is of key importance in
12 the fine chemicals, food and pharmaceutical industries. In this article,
13 a continuous preferential crystallization process is presented that al-
14 lows the separation of conglomerate forming enantiomers in a stable,
15 robust and flexible way. This is achieved by coupling two continuous

This article is dedicated to John M. Prausnitz for his many outstanding contributions to solution thermodynamics and phase equilibria. The new continuous process reported here is based on the properties of ternary phase diagrams for conglomerate forming enantiomers dissolved in solution.

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16 crystallizers by exchanging their clear liquid phases. Each crystallizer
17 is connected to a suspension mill responsible for in-situ seed generation
18 through particle breakage. The dynamic and steady state behavior of
19 this process is extensively analyzed for racemic feed streams through
20 process simulations, and parameter regions, which yield pure enan-
21 tiomers in both crystallizers, are identified. For enriched feed streams
22 we further show when this novel flowsheet is capable of outperforming
23 an ideal batch process in terms of solvent consumption per unit mass
24 of desired enantiopure product produced.

25

26 **Keywords.** separation of enantiomers; continuous crystallization;
27 milling; population balance equation models; process design; threonine

28 **Introduction**

29 Obtaining enantiopure products is important in many industries, e.g., the
30 pharmaceutical, food and fine chemicals industries. In a pharmaceutical
31 product typically only one of the enantiomers is biologically active, while
32 the other enantiomer is either not effective as a drug or even harmful to hu-
33 mans. In such cases, the pharmaceutical industry strives to produce enan-
34 tiomerically pure compounds. Two major routes to enantiopure products
35 are evident: asymmetric chemical synthesis or the separation of enantiomers
36 from an enantiomerically impure starting material. While the former is the
37 more desirable option in terms of raw material consumption, it often does
38 not allow attaining the required purity directly. Therefore, the development
39 of processes that allow separating enantiomers is essential.

40 The two major separation process alternatives in this context are contin-
41 uous chiral chromatography^{1,2} and crystallization processes^{3,4}. An overview
42 of further resolution methods is given in a recent review article by Lorenz
43 and Seidel-Morgenstern⁵. The product resulting from chromatography is a
44 liquid, however, most products in the pharmaceutical, food and fine chem-
45 icals industries are ultimately sold as solids. Hence, there is usually a fur-
46 ther crystallization step necessary to obtain the desired solid particles with
47 high purity. On the other hand, the most commonly used crystallization-
48 based resolution process relies on the formation of two diastereomeric salts
49 that have different physical properties and can thus be crystallized consecu-
50 tively⁶⁻⁸. However, this process requires the molecules to form salts, which
51 is not always possible. It also requires (at least) stoichiometric amounts of a

52 chiral resolving agent, which needs to be separated from the desired product
53 and recycled in further processing steps.

54 From a standpoint of process intensification, specifically the minimiza-
55 tion of energy requirements and solvent consumption, it is appealing to in-
56 vestigate crystallization processes that can separate enantiomers and deliver
57 a solid product in a single process step from a solution containing both enan-
58 tiomers and a solvent⁴. The crystallization strategy to be employed mainly
59 depends (1) on the type of phase diagram for a specific ternary system, (2)
60 whether racemization in solution is possible, and (3) the enantiomeric excess
61 in the feed material^{5,9}. Most ternary phase diagrams of organic enantiomers
62 and a solvent correspond to one of three classes: conglomerates, racemic
63 compound forming systems and solid solutions¹⁰. Qualitative ternary phase
64 diagrams for these three cases are shown in Figure 1 in the form of isother-
65 mal cuts. In that figure, we have indicated the type and number of stable
66 phases in each phase region. The key difference between the different types of
67 phase diagrams lies in the structure of the solid phases that can be obtained.
68 In conglomerates (Figure 1a, around 10% of all cases) the stable crystalline
69 phases consist of either pure S enantiomer or pure R enantiomer. In racemic
70 compound forming systems (Figure 1a, around 90% of all cases), there is
71 additionally a solid racemic compound that consists of equal amounts of
72 R and S enantiomer (designated RS). Fortunately, the case of solid solu-
73 tions (Figure 1c), where crystals can contain any composition of R and S
74 enantiomers and which are hardest to separate¹¹, is rarely encountered for
75 organic molecules. Apart from the ideal cases shown in Figure 1 there are
76 numerous (combinations of) nonidealities possible, e.g., the presence of a

77 metastable conglomerate in racemic compound forming systems¹², partial
78 solid solutions¹³, the presence of liquid-liquid equilibria¹⁴, and the presence
79 of (metastable) polymorphs¹⁵.

80 In this article we will focus our attention on conglomerates. If the enan-
81 tiomeric excess in the feed material is high enough, direct crystallization in
82 the two phase region is possible. This is shown on the right side of Figure 2a
83 for an isothermal batch crystallization. In this process, one starts from a
84 supersaturated initial condition (green circle) and upon nucleation or the
85 introduction of seed crystals of the R enantiomer, one follows the mass bal-
86 ance line (dashed grey line) to the thermodynamic equilibrium (blue square).
87 Clearly, a continuous crystallization process carried out in a mixed suspen-
88 sion, mixed product removal crystallizer (MSMPRC) with feed conditions
89 in the two phase region (green circle in Figure 2b) reaches a steady state
90 operating point (blue square) that lies in the two phase region as well. It is
91 therefore able to produce pure R enantiomer in a continuous fashion.

92 When there is no enantiomeric excess in the feed material, preferential
93 crystallization¹⁶ is one of the most attractive processing alternatives[‡]. The
94 two key concepts that enable preferential crystallization processes are (1)
95 the dependence of mass uptake of solute into the crystalline phase on the
96 surface area of the crystals, i.e., the amount of solute incorporated per unit
97 time depends linearly on the total surface area of the crystals present in the
98 suspension, and (2) the existence of a metastable zone, i.e., the nucleation
99 of new crystals (in this case of the counter-enantiomer) is an activated pro-

[‡]Note that we are primarily interested in cases where racemization of enantiomers in the solution proves difficult. In cases where racemization in solution is more accessible the process of Viedma ripening¹⁷⁻²⁰ becomes relevant.

100 cess and does not readily occur at low supersaturations. In the case of a
101 conglomerate, it therefore becomes possible to preferentially grow crystals
102 of the desired enantiomer through a seeded process. Performing this pro-
103 cess in a batch crystallizer at constant temperature (as shown in the three
104 phase region of Figure 2a), the initially racemic and supersaturated liquid
105 phase (green circle) is depleted of the R enantiomer, which continues until
106 nuclei of the undesired S enantiomer are formed (at this time the process
107 trajectory of the residual liquid composition breaks away from the dashed
108 line). Henceforth, the solution rapidly approaches the thermodynamic equi-
109 librium, i.e., it becomes racemic again, but at the saturation concentration
110 (purple square symbol). An isothermal batch crystallization process based
111 on preferential crystallization would be stopped before the nucleation of
112 crystals of the undesired enantiomer occurs, so that only pure crystals of
113 the desired enantiomer can be collected. Since such a precise stopping of
114 the crystallization process and a quick filtration of the product crystals is
115 cumbersome, preferential crystallization processes can be carried out in a
116 polythermal fashion as described by Levilain and Coquerel²¹ and Levilain
117 et al.²².

118 Recently, advanced continuous processing concepts that allow preferen-
119 tial crystallization processes to be operated at steady state have been de-
120 veloped²²⁻²⁵. In this article, we add to these concepts by presenting a novel
121 processing flowsheet and its rationale (in section “The flowsheet and its
122 rationale”). This flowsheet allows operating continuous preferential crystal-
123 lization processes for a wide range of kinetics (even for cases with a narrow
124 metastable zone for the undesired enantiomer) and with a high yield. This

125 is accomplished through the use of mother liquor recycles (to increase the
126 yield) and heated suspension mills (to generate seed crystals in-situ by break-
127 ing parent particles and to dissolve nuclei of the undesired enantiomer) as
128 described in the next section. We then construct a process model based on
129 population balance equations (in section “Process model”) that allows us to
130 evaluate the dynamic and steady state behavior of the process. In the results
131 and discussion section we will show through extensive process simulations
132 that the flowsheet can be operated in an inherently stable fashion, i.e., that
133 steady states can be found that are approached even from enantiomerically
134 impure initial conditions. The ranges of process parameters where this be-
135 havior is observed are then identified. For the case of enriched feed streams,
136 we identify the conditions where our novel continuous flowsheet is able to
137 produce pure enantiomers with lower solvent requirements than an ideally
138 operated batch crystallization process.

139 **The flowsheet and its rationale**

140 Levilain and Coquerel²¹ described how a single batch crystallizer can be
141 used to obtain the desired enantiomer in a safe and reproducible manner by
142 first crystallizing it as described above and then raising the temperature to
143 dissolve crystals of the undesired enantiomer (and part of the crystals of the
144 desired enantiomer). This concept was subsequently expanded by Levilain
145 et al.²² using two crystallizers in order to couple preferential crystallization
146 and dissolution. Since these crystallizers were initially seeded with opposite
147 enantiomers, the process allowed obtaining both enantiomers in pure form.

148 While such processes where an improvement to the rather unstable batch
149 operation as described in the introduction (text relating to Figure 2a), an
150 important fact was not accounted for: preferential crystallization processes
151 are ideal to be run continuously. The continuous operation of preferential
152 crystallization has the advantage that these kinetically controlled processes
153 can be run at a steady state away from the thermodynamic equilibrium,
154 such that the desired enantiomer is obtained continuously with a high pu-
155 rity and a high yield. A continuous preferential crystallization process was
156 first presented in the open literature by Qamar et al.²³. They treated a sin-
157 gle mixed suspension mixed product removal crystallizer (MSMPRC) with
158 a fines dissolution pipe and numerically investigated the effect of different
159 ratios of residence times (main crystallizer vs. dissolution pipe) and different
160 seeding strategies, i.e., seeds were either introduced continuously or in peri-
161 odic fashion through the feed stream. In a follow-up paper a flowsheet with
162 two coupled crystallizers, which were seeded using opposite enantiomers and
163 which were connected through liquid phase exchange pipes, was presented.²⁴
164 This concept was previously successfully demonstrated — both theoretically
165 and experimentally — for two coupled batch crystallizers^{26,27} As in the case
166 of the two batch crystallizers, the continuous process allowed obtaining both
167 enantiomers in pure form. The continuous process is schematically drawn
168 inside the three phase region of the isothermal phase diagram shown in Fig-
169 ure 2b. In that figure, the green circle represents the feed point, while the
170 square and triangle represent the steady states of the two coupled crystalliz-
171 ers. The exchange of the liquid phase between the two crystallizers mimics
172 its racemization, i.e., the higher the exchange rate between the two crys-

173 tallizers, the closer move the square and triangle to the vertical center line
174 (indicated by the arrows in that figure). The effect of this exchange is an
175 increase in the supersaturation of the preferred enantiomer and decrease in
176 the supersaturation of the undesired enantiomer in each crystallizer, hence
177 leading to a better performance of the process and a broader operating win-
178 dow of the process. However, Qamar et al.^{23, 24} still used continuous or
179 periodic seeding to accomplish their separation performance (in the case of
180 Qamar et al.²⁴ seed crystals for both enantiomers were needed). An ex-
181 perimental implementation of a similar process was presented by Chaaban
182 et al.^{28, 29}, who, however, only treated the liquid phase in a continuous fash-
183 ion and needed to restart their process with fresh seeds after some time.
184 Furthermore, the yield obtained from all three processes was rather low.

185 In this paper, we present a novel flowsheet for continuous preferential
186 crystallization with an increased productivity, in-situ seed generation by
187 particle breakage and an even broader operating window. The overall flow-
188 sheet of such a process is drawn in Figure 3. Similar to Qamar et al.²⁴ the
189 two MSMPRCs are fed from a single feed tank with a clear racemic solution
190 and the two crystallizers exchange liquid phase with each other. However,
191 there are two main novelties in our flowsheet: (1) the use of heated mills for
192 in-situ seed generation and fines dissolution and (2) the inclusion of contin-
193 uous filtration units and recycle streams for the mother liquor separated in
194 the filtration units to increase the process yield. Introducing the suspension
195 mills as shown in Figure 3 enables the in-situ production of seeds by breaking
196 parent particles entering the mills from their respective crystallizers. Natu-
197 rally, other devices that generate additional crystals from parent particles,

198 such as sonicators, could be used for this purpose as well. Furthermore, op-
199 erating the mills at an elevated temperature enables the dissolution of fines
200 particles of the undesired enantiomer, possibly generated by nucleation in
201 the crystallizer. This last point is of key importance because the supersatu-
202 ration of the undesired enantiomer in each crystallizer is *necessarily* higher
203 than for the desired enantiomer unless the liquid phases between the two
204 crystallizers are exchanged at infinitely fast rates, which would lead to total
205 racemization of the liquid phase in each crystallizer. However, this is clearly
206 impossible due to physical constraints on the exchange flow rates between
207 the two crystallizers. Since the supersaturation of the undesired enantiomer
208 is higher, its (homogeneous) nucleation rate must be faster as well. For sys-
209 tems with a narrow metastable zone of the undesired enantiomer this fact
210 becomes problematic, because there is a substantial risk that nuclei of the
211 undesired enantiomer accumulate over time in each crystallizer, such that
212 the system leaves its previous, apparently stable, state rapidly. Ultimately,
213 this would lead to enantiomerically impure products. Our use of suspension
214 mills at an elevated temperature is therefore expected to remove this issue
215 and stabilize the process by generating a large amount of seeds by breaking
216 particles of the desired enantiomer and by dissolving nuclei of the undesired
217 enantiomer.

218 In the following two sections, we will present a process model based
219 on the population balance equation (in section “Process model”) and then
220 investigate, through the use of a copious amount of process simulations at
221 various conditions, whether our rationalization of the flowsheet is accurate
222 (in section “Results and discussion”).

223 **Process model**

224 In order to describe the evolution of the particle size distribution of both
 225 enantiomers in all processing units population balance equations (PBEs) are
 226 used^{30,31}, which are coupled with mass balances for the liquid phase. We
 227 assume that a single characteristic length can describe the particles, that the
 228 crystallizers (C) and mills (M) are well mixed, and that no size classification
 229 occurs at their outlets, so that the particle size distribution in the stream
 230 leaving the processing unit is the same as the particle size distribution inside
 231 the processing unit. The process model detailed below is solved using a high
 232 resolution finite volume scheme as described by Gunawan et al.³², which has
 233 been implemented in MatLAB 2014b³³.

234 **Crystallizer**

235 Additional to the assumptions outlined above, we will assume that no ag-
 236 glomeration and breakage of particles occurs in the crystallizer. With refer-
 237 ence to the overall flowsheet (cf. Figure 3), the population balance equation
 238 for the crystallizer can then be written as

$$\begin{aligned} \frac{\partial n_{C_i}^j(L, t)}{\partial t} = & - \frac{\partial \left(G(S_{C_i}^j, T_{C_i}, L) n_{C_i}^j(L, t) \right)}{\partial L} + \\ & + \frac{1}{m_{C_i}} \left(\dot{m}_{M_i C_i} n_{M_i}^j(L, t) - \dot{m}_{C_i M_i} n_{C_i}^j(L, t) - \dot{m}_{C_i F_i} n_{C_i}^j(L, t) \right) \end{aligned} \quad (1)$$

239 where $n_{C_i}^j(L, t)$ is the number density distribution of particles of enantiomer
 240 $j \in \{R; S\}$ per unit mass of suspension in crystallizer $i \in \{1; 2\}$, L is the
 241 characteristic length of particles, t is the time, G is the crystal growth rate

242 of the particles, $S_{C_i}^j$ is the supersaturation with respect to enantiomer j in
 243 crystallizer i , and T_{C_i} is the temperature in crystallizer i . The first term on
 244 the r.h.s. of Eq. (1) therefore describes the growth kinetics in the crystallizer,
 245 while the further terms characterize the in- and out-flows of particles to
 246 and from the crystallizer. The flow terms are written using the mass flow
 247 rates and the mass of suspension in the crystallizer, e.g., $\dot{m}_{M_i C_i}$ is the mass
 248 flow rate from mill i to crystallizer i and m_{C_i} is the mass of suspension
 249 in crystallizer i (including any solids and liquid). The supersaturation is
 250 defined by:

$$S_{C_i}^j = \frac{c_{C_i}^j}{c_{\star, C_i}^j(T, c_{C_i}^p)} \quad (2)$$

251 where $c_{C_i}^j$ is the concentration of enantiomer j in crystallizer i . The solu-
 252 bility of enantiomer j is designated by $c_{\star, C_i}^j(T, c_{C_i}^p)$, where the superscript
 253 p represents the counter-enantiomer (i.e., $p = R$ for $j = S$ and vice versa).
 254 Note that in Eq. (1) we have assumed that the recycle stream originating
 255 from the filtration unit and the exchange stream originating from the other
 256 crystallizer are particle free and thus do not appear in the PBE. The initial,
 257 boundary and regularity conditions for Eq. (1) can be written as:

$$\begin{aligned}
 n_{C_i}^j(L, t = 0) &= n_{0, C_i}^j(L) \\
 n_{C_i}^j(L = 0, t) &= \frac{J(S_{C_i}^j, T_{C_i})}{G(S_{C_i}^j, T_{C_i}, L = 0)} \\
 n_{C_i}^j(L = \infty, t) &= 0
 \end{aligned} \quad (3)$$

258 where J is the nucleation rate per unit mass of clear liquid and $n_{0, C_i}^j(L)$
 259 is the number density distribution per unit mass of suspension of the seed

260 crystals of enantiomer j in crystallizer i . In order to track the evolution of
 261 the supersaturation of both enantiomers in the crystallizer, the population
 262 balance equation is coupled with a mass balance for the liquid phase:

$$\begin{aligned} \frac{dc_{Ci}^j}{dt} = & -k_v\rho_c \frac{d\mu_{3,Ci}^j}{dt} + \frac{1}{m_{Ci}} \left(\dot{m}_{SCi}c_S^j + \dot{m}_{MiCi}c_{Mi}^j + \dot{m}_{CqCi}c_{Cq}^j + \dot{m}_{FiCi}c_{Fi}^j \right) + \\ & - \frac{1}{m_{Ci}} \left(\dot{m}_{CiCq}c_{Ci}^j + \dot{m}_{CiMi}c_{Ci}^j + \dot{m}_{CiFi}c_{Ci}^j \right) \end{aligned} \quad (4)$$

263 where the concentration of enantiomer j in crystallizer i (c_{Ci}^j) is defined per
 264 mass of clear liquid and we use the subscript q for streams originating from
 265 the other crystallizer (i.e., $q = 2$ for $i = 1$ and vice versa). $\mu_{3,Ci}^j$ is the third
 266 moment of the particle size distribution of enantiomer j in crystallizer i ,
 267 which is defined as

$$\mu_{3,Ci}^j = \int_0^\infty L^3 n_{Ci}^j(L, t) dL \quad (5)$$

268 The initial condition for Eq. (4) is given by $c_{Ci}^j(t = 0) = c_{0,Ci}^j$.

269 Mill

270 The population balance equation for the suspension mills can be written in
 271 a similar fashion, but includes additional terms describing the appearance

272 and disappearance of particles due to breakage:

$$\begin{aligned}
 \frac{\partial n_{M_i}^j(L, t)}{\partial t} = & - \frac{\partial \left(G(S_{M_i}^j, T_{M_i}, L) n_{M_i}^j(L, t) \right)}{\partial L} + \\
 & + \int_L^\infty K(\lambda) d(\lambda, L) n_{M_i}^j(\lambda, t) d\lambda - K(L) n_{M_i}^j(L, t) + \quad (6) \\
 & + \frac{1}{m_{M_i}} \left(\dot{m}_{C_i M_i} n_{C_i}^j(L, t) - \dot{m}_{M_i C_i} n_{M_i}^j(L, t) \right)
 \end{aligned}$$

273 where we have assumed that the liquid phase is supersaturated with re-
 274 spect to enantiomer j . If $S_{M_i}^j < 1$, the growth rate G is replaced with the
 275 (negative) dissolution rate D , which will cause particles to dissolve/shrink.
 276 As mentioned in section “The flowsheet and its rationale”, the tempera-
 277 tures in the mills are typically set to induce complete dissolution of nuclei
 278 of the undesired enantiomer (and *partial* dissolution of crystals of the de-
 279 sired enantiomer). The milling process itself is characterized through the
 280 daughter distribution $d(\lambda, L)$, where $d(\lambda, L)dL$ is the number of fragments
 281 with size between L and $L + dL$ formed from a larger particle of size λ , and
 282 the breakage rate $K(L)$. The initial, boundary and regularity conditions, as
 283 well as the mass balance can be formulated similarly to Eqs. (3) and (4),
 284 respectively.

285 Filtration unit

286 Since this work is not focused on modeling the continuous filtration unit
 287 precisely, we make the simplistic assumption that the filtration unit perfectly
 288 separates crystals from the mother liquor. As can be seen from the flowsheet
 289 in Figure 3 part of the mother liquor is recycled to the crystallizer in order to

290 increase the overall yield of the process. The remaining part of the mother
291 liquor is purged from the system, therefore preventing the build up of any
292 impurities (and solvent).

293 **Constitutive equations**

294 The above description of the process equations is kept rather general. How-
295 ever, in order to arrive at a specific process example, constitutive equations
296 for the solubility, as well as the growth, dissolution and breakage kinetics are
297 necessary. In this paper a case study on the conglomerate forming system of
298 (2S,3R)- and (2R,3S)-threonine crystallized from water will be presented for
299 which some of the necessary data is already available in the literature. In
300 the equations above and the following considerations, we designate the su-
301 perscript S to (2S,3R)-threonine and the superscript R to (2R,3S)-threonine.
302 Where appropriate kinetic data is not available from the literature, we spec-
303 ify the assumptions we made to complete the process model. Note that
304 the constitutive equations are the same for both enantiomers, but their ar-
305 guments (e.g., the supersaturation) differ. The constitutive equations are
306 explained individually in the following sub-sections and are also summarized
307 in Table 1, where all necessary kinetic parameters are included.

308 **Solubility**

309 In order to describe the solubility of both enantiomers in the three phase re-
310 gion of a conglomerate forming system of enantiomers, it is sufficient to know
311 the solubility at racemic composition for different temperatures, $c_{\star,\text{rac}}(T)$.
312 In order to obtain a continuous description, we fitted a second order poly-

313 nomial through previously reported datapoints³⁴:

$$c_{\star,\text{rac}}(T) = k_{c1} + k_{c2}T + k_{c3}T^2 \quad (7)$$

314 where k_{ci} are parameters. The solubility line for each enantiomer, $c_{\star}^j(T, c^p)$,
315 is given by the straight line connecting the solubility at racemic composi-
316 tion and the corner of the ternary phase diagram representing the pure enan-
317 tiomer; as can for example be seen in Figure 1a. It follows that the solubility
318 of enantiomer j depends on the concentration of the counter-enantiomer p .

319 **Crystallization and dissolution kinetics**

320 For the growth and nucleation kinetics, we will largely use the kinetic model
321 for (2S,3R)- and (2R,3S)-threonine reported by Qamar et al.²⁴, however,
322 since we are primarily interested in the process flowsheet and its features,
323 we have taken the liberty to simplify some of the expressions for convenience.
324 The growth and nucleation kinetics and the relevant kinetic constants are
325 reported in Table 1. For the dissolution kinetics we assumed that they follow
326 a simple linear dependence on the undersaturation

$$D = k_d(S - 1) \quad (8)$$

327 **Breakage kinetics**

328 Crystal breakage occurs in the suspension mills through collisions of crys-
329 tals with each other and by intensive contacts of the crystals with parts of
330 the mill. Clearly, the specific type and extent of breakage depends on the

331 type of mill used and its operating parameters. However, for the sake of
 332 this study, we assume that particle breakage can be described as a binary
 333 breakage process, i.e., original particles break in exactly two fragments, but
 334 the fragments are allowed to be of different sizes. Such a breakage process
 335 can, for example, be described using a U-shaped daughter distribution that
 336 is symmetric in volume space²⁰:

$$d(\lambda, L) = 3L^2(2k_{b1} + 1) \left(\frac{2}{\lambda^3}\right)^{2k_{b1}+1} \left(L^3 - \frac{\lambda^3}{2}\right)^{2k_{b1}} \quad (9)$$

337 where k_{b1} is an integer parameter; the larger the value of k_{b1} the bigger
 338 the difference in size between the two fragments formed from the original
 339 particle. For our case study we have assumed that $k_{b1} = 7$, i.e., that the
 340 particle breakage is attrition-like. The breakage kinetics are completed by
 341 specifying a size-dependent breakage rate, $K(L)$:

$$K(L) = k_{b2}L^{k_{b3}} \quad (10)$$

342 **Results and discussion**

343 **Racemic feed streams**

344 **Determination of steady states and their stability**

345 According to a degree of freedom analysis of the overall flowsheet and follow-
 346 ing the assumptions made in section “Process model”, it is only necessary
 347 to specify some of the streams in the flowsheet, while all other quantities
 348 can be calculated using the model equations above and additional material

349 balances over individual process units and parts of the flowsheet. For the
350 purpose of our case study, we choose to specify the following flow rates: the
351 feed flow rate to each crystallizer (\dot{m}_{SCi}), the exchange flow rate between
352 the crystallizers (\dot{m}_{CiCq}), the flow rate from each crystallizer to its attached
353 mill (\dot{m}_{CiMi}), as well as the flow rate from each crystallizer to its filtra-
354 tion unit (\dot{m}_{CiFi}). We also specify the composition of the feed stream (i.e.,
355 the mass fraction of both enantiomers, w_{SCi}^j), the size of each processing
356 unit (in terms of the suspension mass it contains, e.g., m_{Ci}), as well as the
357 temperature in each processing unit (e.g., T_{Ci}).

358 In order to investigate the behavior of the processing flowsheet in Fig-
359 ure 3, we introduce two case studies with different processing parameters.
360 For the first case study, all processing parameters are introduced in Table 2.
361 Note that we chose to keep the processing parameters for both sides of the
362 flowsheet equivalent, so that only the specifications for the left side (crys-
363 tallizer 1, etc.) are given in this table. The second case study uses the
364 same processing parameters with the exception of the exchange flow rate
365 between the two crystallizers. In case study 1, we have selected a substan-
366 tial exchange flow rate between the two crystallizers, while in case study 2
367 we chose to decouple the two crystallizers by setting the exchange flow rate
368 between them to zero (i.e., $\dot{m}_{C1C2} = \dot{m}_{C2C1} = 0$).

369 In order to investigate the transient behavior of the process for these
370 two case studies, we ran a series of dynamic simulations with the process
371 model described in section “Process model”. It is also necessary to specify
372 the initial conditions in each processing unit. This entails specifying the
373 particle size distributions (PSDs) of the seed crystals of both enantiomers,

374 as well as the initial composition of the solution in all processing units. The
 375 PSDs of the seed crystals in the crystallizers are assumed to follow normal
 376 distributions with modal size 100 μm and standard deviation of 20 μm (with
 377 the tail of the distribution extending to negative particle sizes cut off). The
 378 number of seed particles is adjusted to achieve a certain initial enantiomeric
 379 excess and a certain total seed mass. In all simulations presented in this
 380 article, we choose to specify the seed PSDs in the mill and the crystallizer
 381 on the respective side of the flowsheet to be the same. Furthermore, we
 382 specify the initial conditions to be “mirror-symmetric” across the two sides
 383 of the flowsheet. To properly specify the enantiomeric purity of the seeds,
 384 we define the time-dependent solid state enantiomeric excess in crystallizer
 385 i as:

$$\epsilon_{s,C_i}(t) = \frac{\mu_{3,C_i}^R(t) - \mu_{3,C_i}^S(t)}{\mu_{3,C_i}^R(t) + \mu_{3,C_i}^S(t)} \quad (11)$$

386 Using this definition the specifications on the seed PSDs become:

$$\begin{aligned} \epsilon_{s,C1}(0) &= -\epsilon_{s,C2}(0) \\ \mu_{3,C1}^R(0) + \mu_{3,s,C1}^S(0) &= \mu_{3,C2}^R(0) + \mu_{3,C2}^S(0) \\ \mu_{3,M_i}^j(0) &= \mu_{3,C_i}^j(0) \end{aligned} \quad (12)$$

387 The initial composition of the solution in all vessels is taken to be the same
 388 as in the feed stream (cf. Table 2), i.e., in this case it is racemic and super-
 389 saturated.

390 Now that we have specified all particulars of case studies 1 and 2, we
 391 can investigate the dynamic behavior of the flowsheet in both cases in order
 392 to investigate potential steady states and their stability. To this end, we

393 report the evolution of the solid state enantiomeric excess in crystallizer 1,
394 $\epsilon_{s,C1}(t)$, starting from initial values of $\epsilon_{s,C1}(0) = \{1; 0.7; 0.5; 0.33; 0\}$ (from
395 enantiomerically pure seed material to racemic seed material) in Figure 4.
396 Focusing first on case study 1 (Figure 4a), where we specified a substantial
397 solution exchange flow rate between the crystallizers, we see that the solid
398 state enantiomeric excess approaches unity for all cases except for the case
399 where we started in perfectly racemic conditions ($\epsilon_{s,C1}(0) = 0$, solid blue
400 line). Since the flowsheet is completely symmetric in this case, this indi-
401 cates that we can obtain the pure desired enantiomer from crystallizer 1
402 and the pure counter-enantiomer from crystallizer 2. Note that in all cases
403 with an initial solid state enantiomeric excess we first observe a decrease in
404 enantiomeric excess before the system recovers and reaches the pure steady
405 state. This is caused by the selection of the initial solution state. Since it is
406 racemic, but strongly supersaturated, crystals of both enantiomers nucleate
407 initially, which decreases the enantiomeric excess. It is especially noteworthy
408 that under these conditions the flowsheet is able to reject large amounts of
409 enantiomeric impurities that are present in the initial seed material. From
410 this analysis, we can surmise that there must be (at least) two steady states
411 for case study 1: a stable steady state yielding the desired and counter-
412 enantiomer in pure form from the respective crystallizer and an unstable
413 steady state yielding both enantiomers in racemic composition from both
414 crystallizers. This inherently stable behavior stands in stark contrast to
415 any batch process using preferential crystallization. In such batch processes
416 even a slight amount of enantiomeric impurity in the seed material alters the
417 trajectory significantly for the worse; especially when secondary nucleation

418 kinetics are significant.

419 Turning our attention now to case study 2 (Figure 4b), where we specified
420 the crystallizers to be decoupled (without solution exchange between them),
421 we see that all trajectories are converging to the racemic steady state, except
422 for the one that already starts at full enantiomeric purity (i.e., $\epsilon_{s,C1}(0) = 1$,
423 solid black line). Thus, the steady state stability in this case study is exactly
424 reversed from case study 1: the racemic steady state is the stable one, while
425 the enantiopure steady state is the unstable one. Additionally to the process
426 simulations shown in Figure 4b, we have also conducted simulations for
427 much longer times (> 400 hours) with only minor amounts of enantiomeric
428 impurity (< 1 wt% of total seed mass) present in the initial state. Even in
429 these cases, the simulations converged to the racemic steady state. Note that
430 while the steady state behavior is exactly reversed in case studies 1 and 2,
431 the dynamic approach to the respective steady states occurs generally much
432 faster in case study 2 at comparable levels of enantiomeric impurity. From
433 this investigation we conclude that a significant exchange rate between the
434 two crystallizers, which racemizes the composition of the solution phase
435 and therefore reduces the supersaturation of the counter-enantiomer in each
436 crystallizer, is able to stabilize the enantiopure steady state significantly.
437 We consider operating the process in such an inherently stable fashion to
438 be highly beneficial when aiming for enantiopure products via continuous
439 preferential crystallization.

440 **Time to steady state**

441 In the previous section we identified that different seed purities alter the
442 time required to reach the enantiopure steady state in case study 1. It
443 seems evident that also the overall seed mass added to the processing units
444 will influence the time required to reach steady state. In order to further
445 investigate this effect, we now report simulations with varying enantiomeric
446 excess in the feed material and varying total seed mass, while all other
447 conditions are kept as in case study 1. We converged all these process
448 simulations to their enantiopure steady state and report the time to steady
449 state as the last time at which the enantiomeric excess in the solid phase is
450 smaller than 0.99 in crystallizer 1 (and thus greater than -0.99 in crystallizer
451 2). The resulting data are shown in Figure 5, where the time to steady state
452 (color scale) is reported with respect to the relative seed mass (normalized
453 by the expected yield at steady state) and the enantiomeric excess present
454 in the seed material.

455 From that figure we can see that a high enantiomeric purity in the seed
456 material yields a much shorter time to steady state. The total seed mass on
457 the other hand does not change the time to steady state significantly. This
458 is a consequence of how we have defined the time to steady state: we have
459 exclusively focused on the time that is required to obtain an enantiomeri-
460 cally pure solid product from the two crystallizers, while we have chosen to
461 neglect all liquid phase properties in the crystallizers. If massive amounts
462 of seeds are supplied to the crystallizers, the supersaturation in the crys-
463 tallizers crashes to a low value and only slowly recovers to its steady state

464 value (something that one might term “over-seeding”). Vice versa, if the
465 seed amount is chosen to be small, the supersaturation in the liquid phase
466 takes longer to sink to the steady state supersaturation, which could be re-
467 ferred to as “under-seeding”. However, our definition of the time to steady
468 state does not include such considerations because we are focusing on the
469 enantiomeric purity in the obtained product streams exclusively.

470 **Identification of process parameters that yield enantiopure prod-** 471 **ucts**

472 In section “Determination of steady states and their stability” we identified
473 two possible outcomes of steady state stability of the overall flowsheet, which
474 were identified by changing the exchange flow rate between the crystallizers.
475 It would seem logical that the residence time in the crystallizers, which is
476 chiefly affected by the outlet flow rate to the filtration units (\dot{m}_{CiFi}), will
477 influence the stability of the steady states as well. In order to show this
478 effect, we have carried out additional process simulations varying these flow
479 rates at otherwise identical conditions to case study 1 (cf. Table 2). For
480 this analysis, we have conducted process simulations starting from an ini-
481 tial solid state enantiomeric excess ($\epsilon_{s,C1}(0) = 0.5$ and $\epsilon_{s,C2}(0) = -0.5$)
482 and have varied the exchange flow rates (\dot{m}_{CiCp}) and outlet flow rates from
483 the crystallizers to the filtration units (\dot{m}_{CiFi}) and subsequently determined
484 the stable steady state for these process configurations. The results are re-
485 ported in Figure 6a where we indicate the processing conditions that lead
486 to enantiomerically pure products as the green region and the processing
487 conditions that yield a racemic solid state product as the grey region. In

488 order to create this plot, we ran 400 simulations for a total process time of 50
489 hours with the relevant flow rates distributed on a linear grid. Note that for
490 some of these flow rate combinations the simulations did not yet converge to
491 either the racemic ($\epsilon_{s,C1}(t = 50 \text{ h}) \geq 0.01$) or the enantiopure steady state
492 ($\epsilon_{s,C1}(t = 50 \text{ h}) \leq 0.99$). While there was a clear tendency to which outcome
493 would eventually prevail in these simulations, we refrain from assigning them
494 to either the grey or the green region and report them as the striped region
495 in Figure 6a. By extending these simulations to longer processing times,
496 we could eventually determine their outcome, but we deemed the computa-
497 tional effort for this exercise to be unreasonably high. Furthermore, such
498 process conditions, where the steady state is approached very slowly, are
499 inherently unattractive and should be avoided. Regardless, from Figure 6a
500 we gather that there is a considerable range of processing conditions where
501 an enantiopure product (green region) can indeed be obtained; including
502 processing conditions with reasonable values for all flow rates. Two further
503 points are worth making with respect to the shape of the green region in Fig-
504 ure 6a: first, we could identify that there is a threshold exchange flow rate
505 between the two crystallizers which enables obtaining enantiopure products.
506 However, this threshold occurs at increasingly small residence times of the
507 particles in the crystallizer (large outlet flow rates). One could conjecture
508 that the threshold exchange flow rate might be asymptotically decreased
509 to zero for even larger outlet flow rates. Since this condition is equivalent
510 to a short particle residence time in the crystallizer, these process condi-
511 tions would involve increasingly massive recycle flow rates for the mother
512 liquor if an acceptable yield were still to be obtained. Hence, such process-

513 ing conditions are impractical. Second, the exchange flow rate required to
514 obtain an enantiomerically pure product at small outlet flow rates (large
515 particle residence times in the crystallizer) increases rapidly. This indicates
516 that a similarly impractical behavior for long particle residence times ex-
517 ists as well, i.e., for these long particle residence times an increasingly large
518 exchange flow rate is needed to stabilize the process sufficiently.

519 In order to investigate the effect of further processing conditions, we
520 also varied the temperature and size of the suspension mills, as reported in
521 Figures 6b to 6f. Raising the temperature in the suspension mills affects
522 the process by providing a higher driving force for the dissolution of fine
523 particles and increasing the size of the mills increases the residence time in
524 the mills (therefore allowing more time for particles to get milled and more
525 time for nuclei to dissolve). Both of these effects should impact the stability
526 of the process positively, however, these changes also negatively impact the
527 productivity of the process (if the recycle/purge ratio for the mother liquor
528 is kept constant). Indeed, in the above-mentioned additional subfigures of
529 Figure 6, we see that the green region, where enantiomerically pure products
530 can be obtained, changes its position in the exchange flow rate vs. outlet
531 flow rate plane. However, it is noteworthy that the same general behavior
532 for the shape of the green region is observed, therefore further substantiating
533 the observations made before. Further analyzing the data shown in these
534 figures, we see that an increase in the suspension mill temperature shifts
535 the green region towards lower outlet flow rates and lower exchange flow
536 rates (lower left of the plane), which indicates that a wider range of realistic
537 flow rates allows obtaining enantiomerically pure products. An increase in

538 the mill's size (increase in residence time in the mill) on the other hand
539 shifts the green region towards lower exchange flow rates, but higher outlet
540 flow rates (bottom right corner of the plane). This indicates that providing
541 the additional residence time in the mill at temperatures higher than in
542 the crystallizer might help with the dissolution of undesired nuclei of the
543 counter-enantiomer, but it also allows more time for small particles of the
544 desired enantiomer to dissolve, which at the same time are produced in
545 greater numbers because there is also more time for particle breakage in the
546 mill.

547 **Investigation of enriched feed streams**

548 In the cases discussed so far we have always supplied a racemic feed stream
549 to the processing flowsheet and showed that enantiopure products can be
550 obtained from such streams in a wide range of processing conditions. How-
551 ever, the feed stream supplied to a crystallization process might already have
552 undergone some kind of enrichment in the desired enantiomer (e.g., by asym-
553 metric synthesis or another separation process). Therefore, it seems prudent
554 to investigate the performance of our continuous preferential crystallization
555 flowsheet for these cases as well. Hence, we introduce process simulations
556 with enriched feed streams with compositions that still lie within the three
557 phase region of the ternary phase diagram at a given temperature. At this
558 point it is noteworthy that such an enantiomerically enriched composition
559 can always be shifted into the two phase region for a conglomerate by either
560 increasing the temperature or removing solvent selectively (e.g., by distilla-
561 tion). To illustrate this in Figure 7, we have drawn the case where we have

562 increased the temperature (red phase boundaries) for a batch vessel in such
563 a way that the initial feed composition (green circle) lies at the border of
564 the two phase region. In this case the optimal yield of a batch crystallizer
565 operated in such a fashion is indicated by the orange square in the diagram.
566 Note that this is the only thermodynamically stable fashion to operate a
567 batch crystallizer that guarantees obtaining an enantiomerically pure prod-
568 uct (barring any non-idealities, such as inclusions of the counter-enantiomer
569 in the crystals). Solvent removal by distillation on the other hand might not
570 be desirable due to potential thermal degradation of the product or simply
571 because of the additional energy requirements that such a process entails.

572 In contrast, the continuous preferential crystallization process can be
573 operated in a stable fashion in the three phase region of the diagram (as
574 already shown for racemic feed streams above) and is thus allowed to operate
575 at a lower temperature (blue phase boundaries). Ideally, the continuous
576 process would therefore be able to reach the steady state condition at the
577 grey triangle (which is just barely supersaturated at the lower temperature),
578 i.e., potentially leading to a higher yield.

579 Operating the continuous preferential crystallization flowsheet in Fig-
580 ure 3 with enantiomerically enriched feed streams entails altering the way the
581 crystallizers are fed. Specifically, introducing the enriched feed stream exclu-
582 sively into the crystallizer producing crystals of the enantiomer in which the
583 feed stream is already enriched is preferable (so that no feed stream enters
584 the second crystallizer, i.e., $\dot{m}_{SC2} = 0$). The second crystallizer producing
585 the crystals of the counter-enantiomer is then fed by an increased exchange
586 flow rate from the first crystallizer, i.e., we specify $\dot{m}_{C1C2} > \dot{m}_{C2C1}$. Conse-

587 quently, since a lower amount of counter-enantiomer needs to be removed,
588 the processing units that produce crystals of the counter-enantiomer can be
589 scaled down. In the following we will scale down the size of the processing
590 units involved in the production of the counter-enantiomer crystals with a
591 scaling factor s defined as:

$$s = \frac{m_{C2}}{m_{C1}} \quad (13)$$

592 We will further use the same scaling factor to scale the flow rates on that
593 side of the flowsheet. For the outlet flow rate from the primary crystallizer
594 to its filtration unit and the exchange flow rate between the crystallizers,
595 we would like to select values that lie within the green region determined
596 for the racemic feed streams (cf. Figure 6). However, at low values of s
597 (i.e., a small crystallizer for the counter-enantiomer producing side), it be-
598 comes unrealistic to draw significant liquid streams from it (even though it
599 becomes replaced by an appropriate incoming stream), as this would result
600 in unrealistic short liquid phase residence times in the small crystallizer.
601 Consequently, we decided to scale the exchange flow rates between the crys-
602 tallizers with the scaling factor as well. An overview of processing parame-
603 ters for the simulations using the enriched feed streams resulting from these
604 considerations is reported in Table 3.

605 **Towards a scaling law for the process**

606 In the following, we investigate the steady state outcome of the continuous
607 crystallization flowsheet for different feed enantiomeric excesses and different
608 scaling factors using the scaled process streams and sizes of processing vessels

609 reported in Table 3. For this purpose, the feed enantiomeric excess, ϵ_f , is
610 defined as

$$\epsilon_f = \frac{w_{\text{SC1}}^{\text{R}} - w_{\text{SC1}}^{\text{S}}}{w_{\text{SC1}}^{\text{R}} + w_{\text{SC1}}^{\text{S}}} \quad (14)$$

611 In Figure 8 we report the solid state enantiomeric excess at steady state ob-
612 tained in the main crystallizer (C1) vs. the scaling factor s for feed streams
613 with different enantiomeric excesses, ϵ_f . Focusing first on the case with
614 a modestly enriched feed stream ($\epsilon_f = 0.125$; blue triangles) we see that
615 an enantiomerically pure product can only be obtained with scaling factors
616 near unity, i.e., the processing units producing the counter-enantiomer are
617 required to be of almost equal size to the processing units producing the de-
618 sired enantiomer. Further downscaling of the processing units on the r.h.s.
619 in the flowsheet leads to a drop in solid state enantiomeric excess obtained
620 at the steady state. Note that we only report the solid state enantiomeric
621 excess at the steady state for the larger crystallizer in Figure 8, however,
622 the smaller crystallizer reached enantiomeric purity as well (with respect to
623 the counter enantiomer, i.e., $\epsilon_{s,\text{C2}}(t_{\text{ss}}) \leq -0.99$). Additionally, we report the
624 solid state enantiomeric excess that would be obtained from a batch crys-
625 tallizer reaching the thermodynamic equilibrium as the dashed lines in that
626 figure. The continuous process on the other hand does *not* reach the thermo-
627 dynamic equilibrium, i.e., the steady state is slightly supersaturated for both
628 enantiomers. This leads to higher solid state enantiomeric excess in the con-
629 tinuous process even when the processing units on the counter-enantiomer
630 side of the flowsheet are scaled down beyond the minimum scaling factor
631 that guarantees enantiomerically pure solids. Focusing now on the addi-

632 tional lines at higher feed enantiomeric excesses ($\epsilon_f = \{0.250; 0.375; 0.500\}$;
633 red green and black symbols, respectively), we see that the minimum scaling
634 factor leading to enantiomerically pure solids decreases with increasing feed
635 enantiomeric excess, as one might have expected.

636 Performing this investigation for additional values of the feed enan-
637 tiomeric excess, we can obtain a series of minimum scaling factors, s_{\min} .
638 We report these minimum scaling factors extracted from this extended se-
639 ries of simulations as the data points in Figure 9. These data points can be
640 well described by a second order polynomial, which is reported in the same
641 figure. This polynomial can be used as an empirical scaling rule for the
642 process flowsheet to decide the minimum size of the processing vessels for
643 the counter-enantiomer side of the flowsheet, which still guarantees enan-
644 tiomerically pure products. Note that this scaling rule is only valid for the
645 crystallization and breakage kinetics listed in Table 1 and the processing
646 and scaling conditions reported in Table 3. Altering these parameters or
647 the kinetics will result in a modified scaling law as well.

648 **Comparison with batch crystallization**

649 The viability of the new continuous process flowsheet in Figure 3 is clear
650 for racemic feed streams for a conglomerate forming system of enantiomers
651 since a batch process cannot reach enantiomeric purity in that case, i.e.,
652 in its thermodynamic equilibrium the batch process will always yield equal
653 amounts of both enantiomers (apart from any seed material that is intro-
654 duced) when starting from a racemic initial point. However, as detailed pre-
655 viously (cf. Figure 7), the application of the designed continuous flowsheets

656 to enantiomerically enriched feed streams needs to be justified, because a
 657 crystallization process carried out in a batch can always be shifted to the two
 658 phase region of the ternary phase diagram by increasing the temperature.
 659 This begs the question: In which cases is running the continuous prefer-
 660 ential crystallization flowsheet beneficial for enantiomerically enriched feed
 661 streams? To give an answer to this question, we will define the efficiency of
 662 the overall continuous process as:

$$\eta_{\text{continuous}} = \frac{k_v \rho_c \mu_{3,\text{C1}}^{\text{R}}(t_{ss})}{m_{\text{C1}} + m_{\text{M1}} + m_{\text{C2}} + m_{\text{M2}}} \quad (15)$$

663 That is, we define the efficiency $\eta_{\text{continuous}}$ as the mass of desired enantiomer
 664 obtained in crystallizer 1 at steady state divided by the mass of suspension
 665 in all processing vessels in the flowsheet. The efficiency defined in this way is
 666 a proxy for the mass of solvent needed to obtain a given mass of the desired
 667 enantiomer in enantiopure form. Similarly, we can define the efficiency of
 668 an ideal batch process (as defined above) as:

$$\eta_{\text{batch}} = \frac{k_v \rho_c \mu_{3,\text{batch}}^{\text{R}}}{m_{\text{batch}}} \quad (16)$$

669 which can be calculated assuming that a batch operated just inside the
 670 two phase region eventually reaches the thermodynamic equilibrium. Us-
 671 ing the scaling rule presented in the previous section, we can determine
 672 the efficiency for the continuous flowsheet at various enantiomeric excesses
 673 and likewise for the batch by determining the temperature rise required
 674 to reach the two phase region of the phase diagram (which is concomitant

675 with a yield loss). We report the resulting efficiencies in Figure 10. One
676 can see that the continuous flowsheet outperforms the batch process at low
677 to moderate enantiomeric excesses in the flowsheet (up to $\epsilon_f \approx 0.35$). For
678 higher enantiomeric excesses an ideal batch process is the more efficient pro-
679 cessing variant. Note that the efficiency curves should not be extrapolated
680 to racemic feed streams/initial conditions ($\epsilon_f = 0$), as the thermodynami-
681 cally stable operation of a batch crystallization process becomes infeasible
682 for a racemic starting condition, i.e., the continuous preferential crystalliza-
683 tion process outperforms batch crystallization processes by definition at this
684 point. While the results shown in Figure 10 suggest a potentially higher ef-
685 ficiency for the continuous preferential crystallization process presented in
686 this article when compared to an ideal batch crystallization process, the
687 continuous process also comes at the expense of an increased operational
688 complexity. Obviously, this added complexity needs to be carefully bal-
689 anced with the gain in efficiency together with the gain in productivity due
690 to steady continuous production of the desired enantiomer.

691 **Practical considerations and alternatives**

692 At this point we would like to point out some practical considerations with
693 respect to an experimental implementation of the proposed continuous flow-
694 sheet and present some additional alternatives. First, the proposed flowsheet
695 requires pumping suspensions, which can be challenging when a substantial
696 residence time is required in the crystallizer and the mill. For a laboratory
697 scale or low tonnage production scale implementation, the challenge stems
698 from the associated small volumetric flow rates. In wide pipes this would

699 lead to a small flow velocity, which could lead to the settling of particles
700 in the pipes (and eventual blockages). Narrower pipes with higher flow ve-
701 locities would, however, also likely be subject to clogging, as the diameter
702 to particle size ratio becomes too small. However, this problem can be cir-
703 cumvented without severe consequences on the “steady state” behavior by
704 using intermittent flow^{35,36}. Second, piping, where undesired nucleation or
705 dissolution could occur, would need to be appropriately insulated or tem-
706 perature controlled. On a laboratory scale this could be accomplished by a
707 tube-in-tube configuration, as for example demonstrated by Galan et al.²⁵.
708 Third, it is noteworthy that there exist several alternatives to our proposal
709 using heated mills and filtered exchange streams between the crystallizers.
710 Instead of generating new particles by breaking existing ones in a mill, one
711 could also use an ultrasound source in the crystallizer to induce crystal frag-
712 mentation³⁷. One could also imagine to promote secondary nucleation of
713 the desired enantiomer. However, the dissolution of undesired nuclei of the
714 counter-enantiomer would still need to be accomplished to achieve the pro-
715 cess stability observed in the implementation presented in this manuscript.
716 This could, for example, be accomplished by a heated fines dissolution loop.
717 Instead of using filtered exchange streams between the crystallizers, one
718 could rely on sequestration based on the hydrodynamics of the crystallizer;
719 a strategy that has recently been realized for Grignard reactions in contin-
720 uous stirred tank reactors.³⁸

721 **Concluding Remarks**

722 In this article we have presented a novel continuous preferential crystalliza-
723 tion process using two crystallizers that are coupled by exchanging their
724 clear liquid phases with each other. Furthermore, the flowsheet involves the
725 in-situ generation of seed particles using suspension mills (or an equivalent
726 device), which concomittantly may act as fines dissolution units. We have
727 shown that this flowsheet leads to enantiomerically pure products in both
728 crystallizers and that it can be operated in an inherently stable fashion, i.e.,
729 an enantiomerically pure steady state can be obtained even from impure
730 initial states. This suggests that the presented process is self-regulating be-
731 cause it will also recover from the sudden appearance of undesired “seeds” of
732 the counter-enantiomer in the crystallizers, which is a phenomenon encoun-
733 tered from time to time in industrial crystallizers due to scale formation at
734 the crystallizer walls. The presented process can therefore be considered to
735 be inherently stable if the processing parameters are correctly chosen. To
736 this end, we have further identified parameter regions that allow obtaining
737 the desired enantiomer in pure form.

738 While these findings are clearly dependent on the particulars of the spe-
739 cific case study (e.g., the crystallization and breakage kinetics), the presented
740 flowsheet is highly adaptable and should allow overcoming adverse kinetics
741 by tuning the milling intensity, temperatures, etc. While tuning the many
742 degrees of freedom in the flowsheet blindly in experimental studies is clearly
743 ill advised, the process model presented in this article may be used as a
744 tool to understand how the process might react to changes in these param-

745 eters, therefore enabling a proper design and deeper understanding of the
746 underlying process.

747 For the case of enriched feed streams we revealed a scaling law for the
748 process and have shown that the continuous process outperforms a batch
749 crystallization process (operated in a thermodynamically stable fashion in
750 the two phase region of the phase diagram) in terms of solvent consumption
751 per mass of enantiopure product. However, this finding is only true in a
752 limited range of feed enantiomeric excesses and comes at the expense of
753 a higher operational complexity. Nonetheless, unveiling and appreciating
754 these tradeoffs enables an informed decision, which is desirable *per se*.

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758 Notation

c	concentration (mass solute per mass of solvent)	[kg kg ⁻¹]
c_*	solubility (mass solute per mass of solvent)	[kg kg ⁻¹]
d	daughter distribution	[m ⁻¹]
D	dissolution rate	[m s ⁻¹]
G	crystal growth rate	[m s ⁻¹]
J	nucleation rate (per mass of clear liquid)	[kg ⁻¹ s ⁻¹]
k	kinetic/thermodynamic parameters	[varies]

K	breakage rate	$[\text{s}^{-1}]$
L	crystal size	$[\text{m}]$
m	suspension mass	$[\text{kg}]$
n	number density distribution (per mass of suspension)	$[\text{kg}^{-1} \text{m}^{-1}]$
\dot{m}	mass flow rate	$[\text{kg s}^{-1}]$
s	scaling factor	$[-]$
S	supersaturation	$[-]$
t	time	$[\text{s}]$
T	temperature	$[\text{K}]$
w	weight fraction	$[-]$
ϵ	enantiomeric excess	$[-]$
η	efficiency	$[-]$
λ	size of parent particle	$[\text{m}]$
μ_3	third moment of PSD	$[\text{m}^3 \text{kg}^{-1}]$
ρ_c	crystal density	$[\text{kg m}^{-3}]$

Superscripts

j	enantiomer
p	counter-enantiomer

Subscripts

C_i	i^{th} crystallizer
-------	------------------------------

f	feed
F_i	i^{th} filtration unit
M_i	i^{th} milling unit
min	minimum
O	outlet (solids)
prim	primary
P	purge (clear liquid)
q	processing unit on opposite flowsheet side
rac	racemic
s	solid state
S	source (feed vessel)
sec	secondary
ss	steady state

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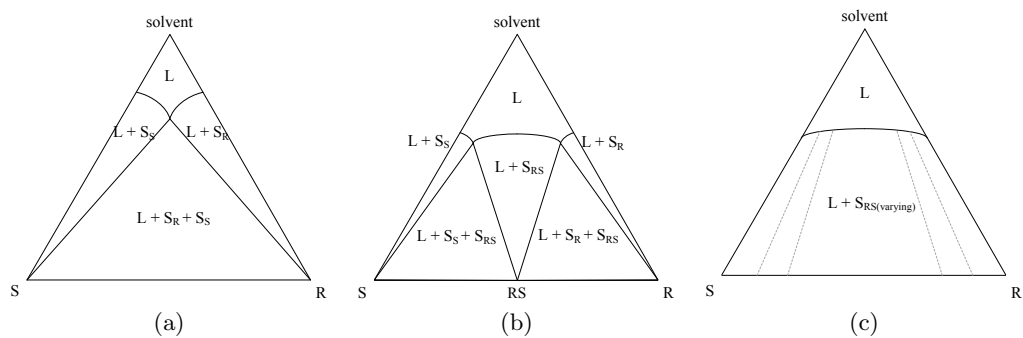


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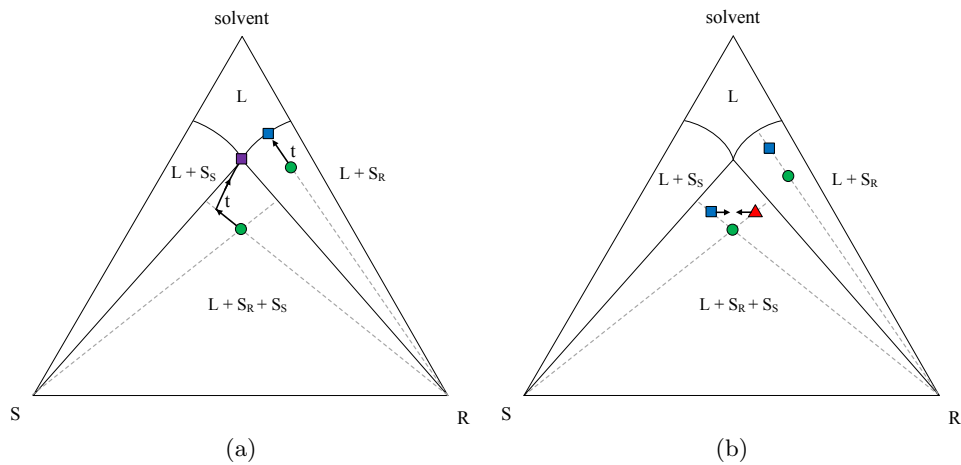


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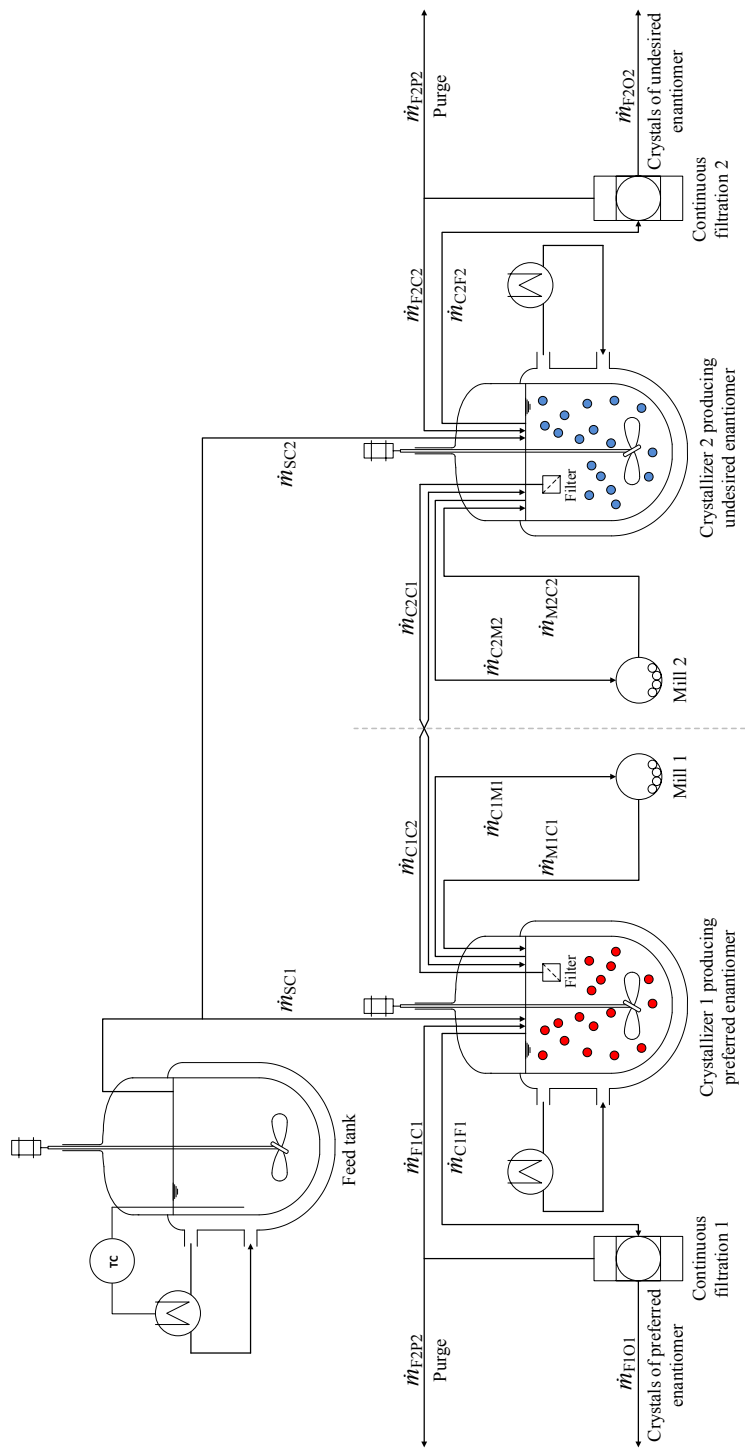


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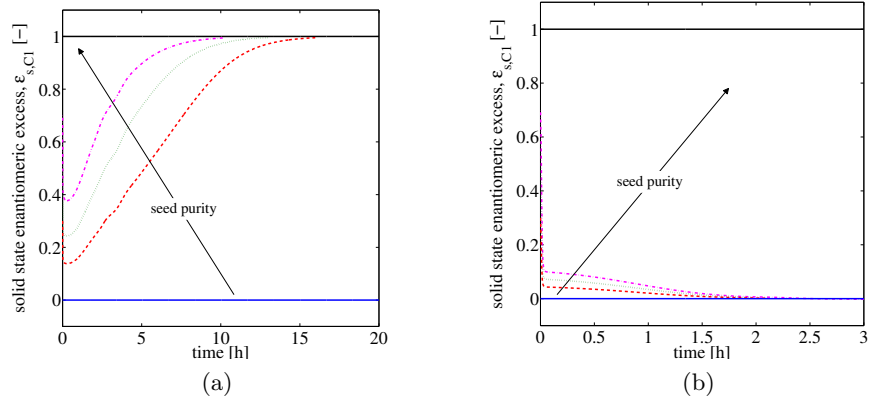


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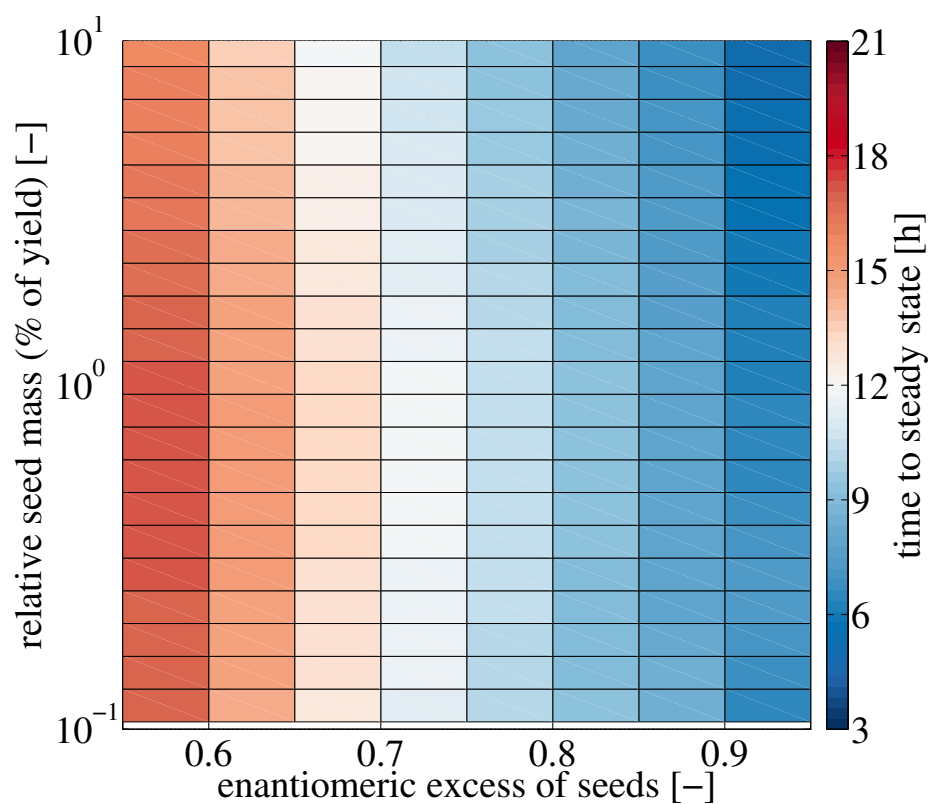


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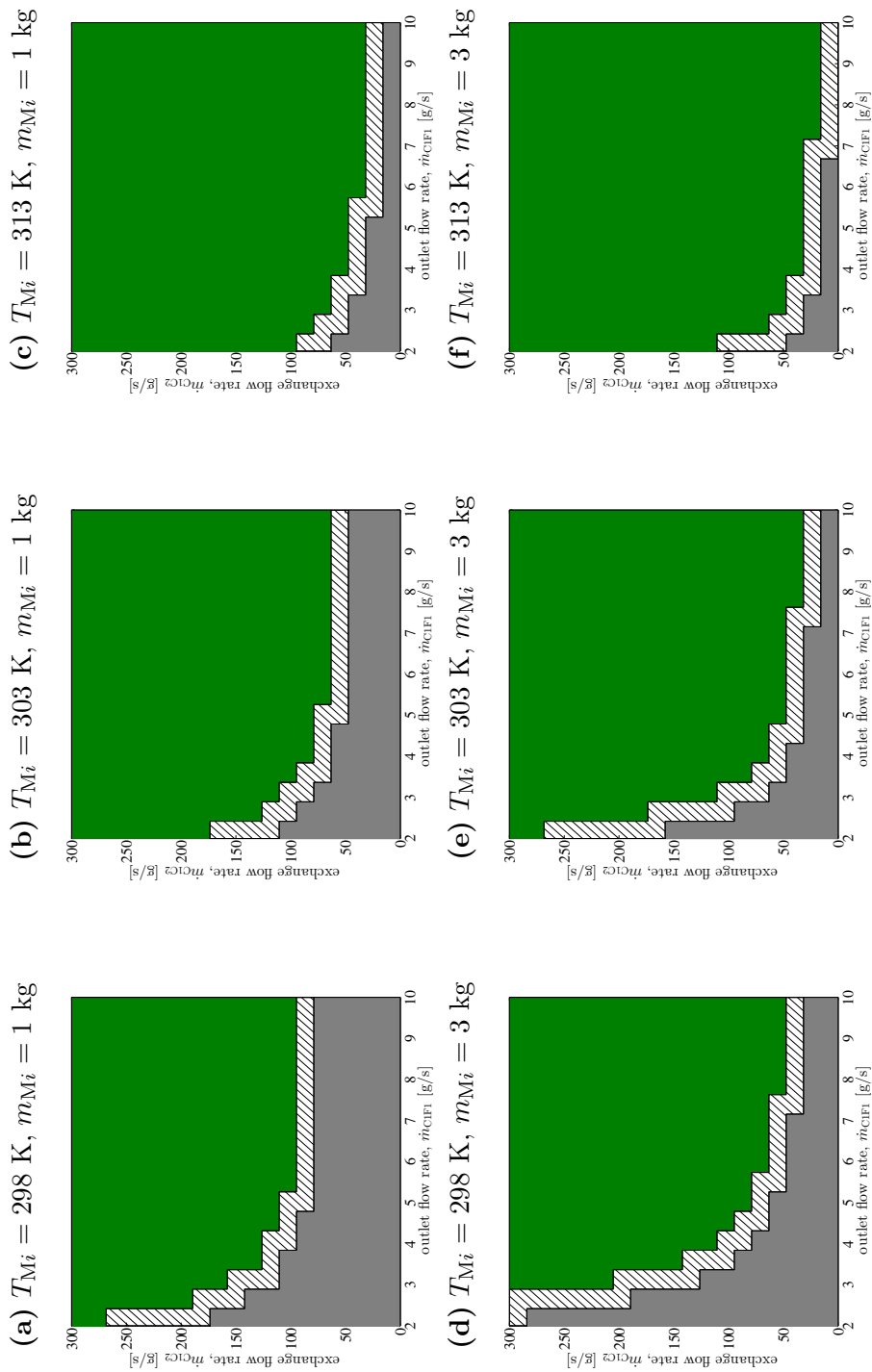


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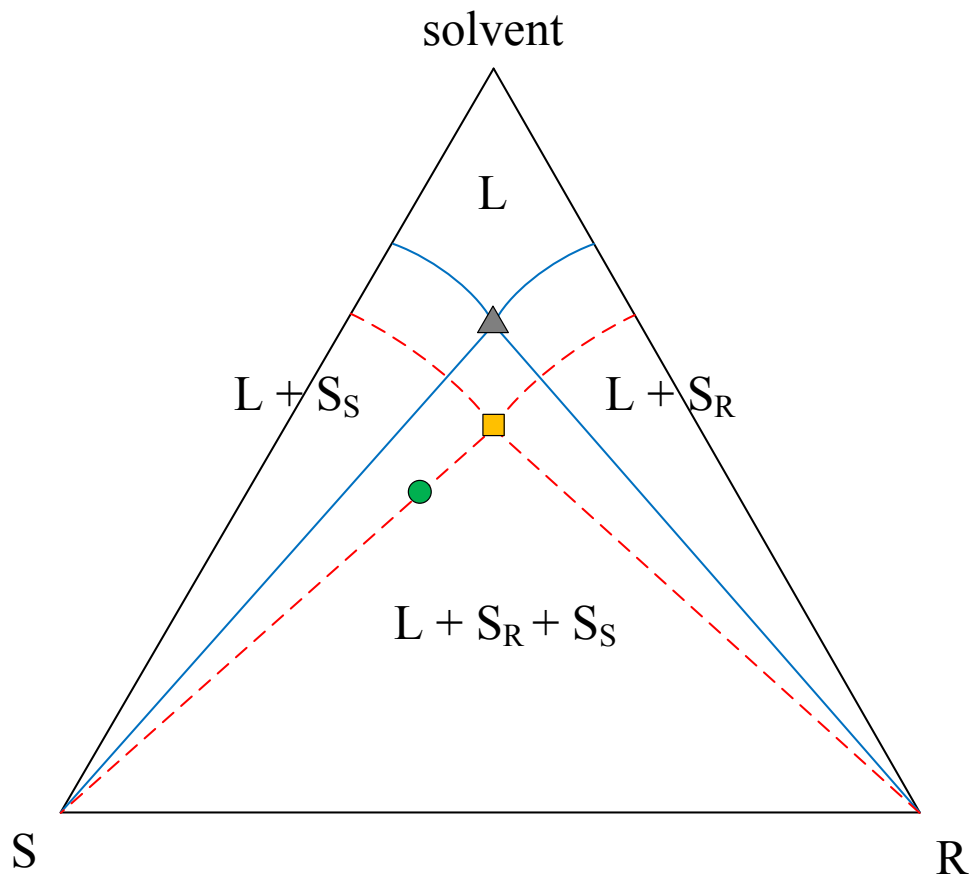


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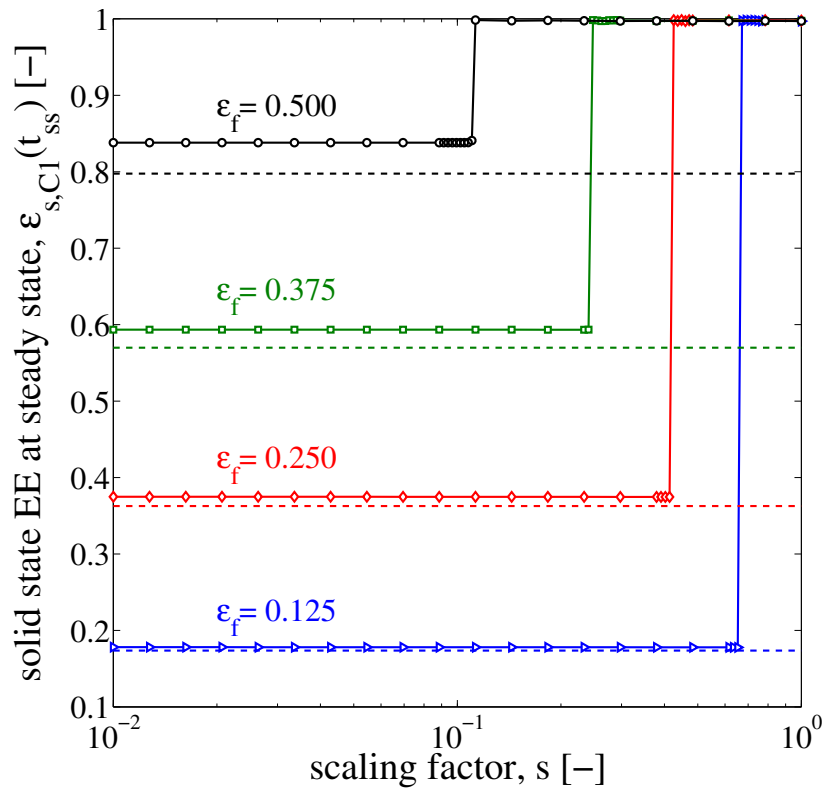


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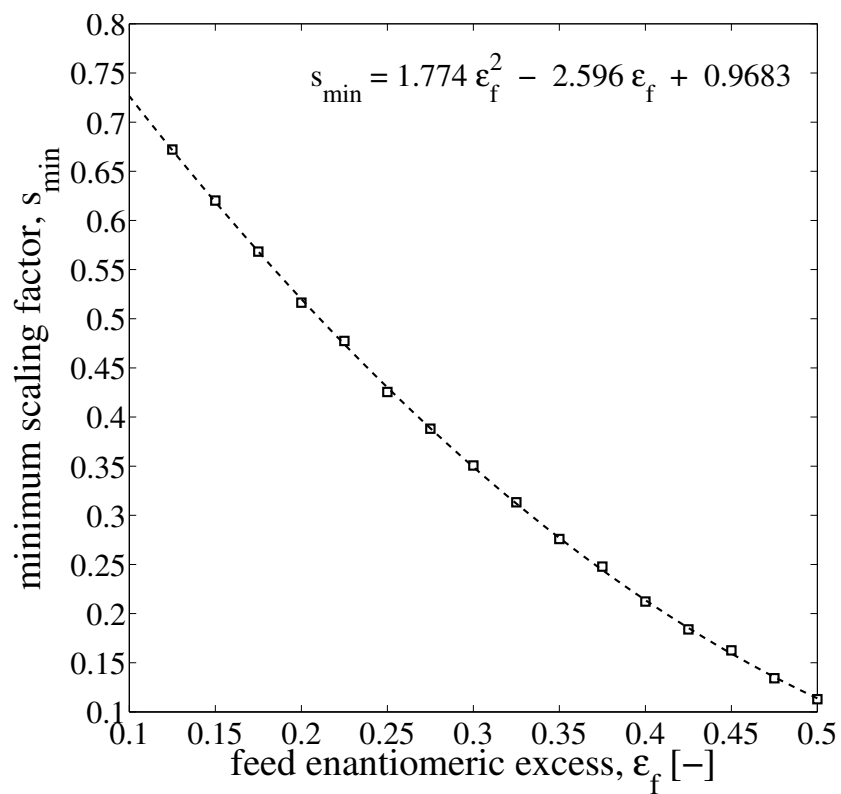


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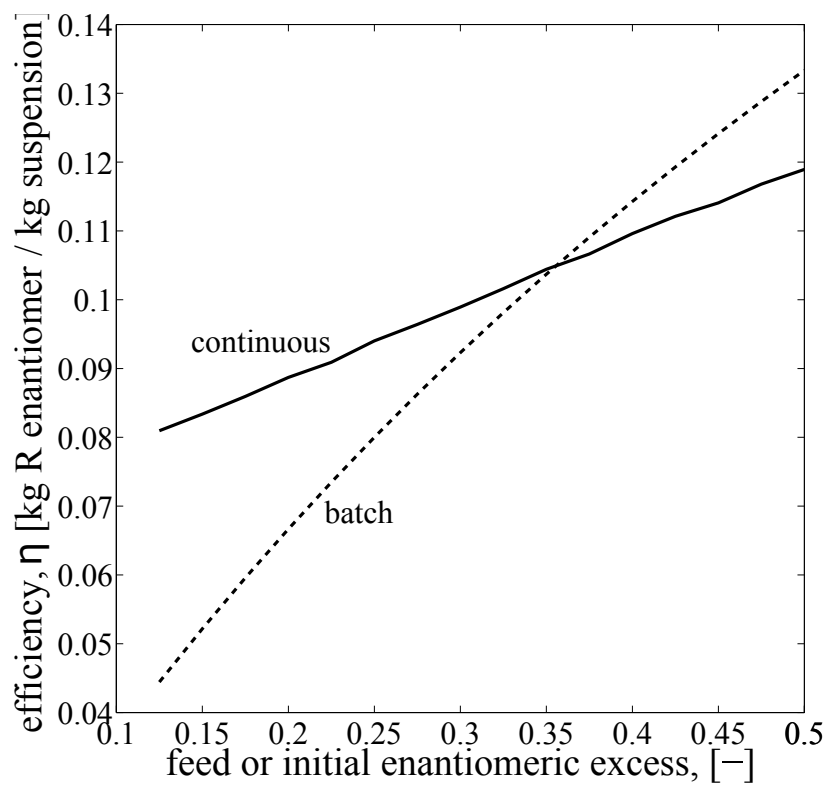


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Table 1: Substance data used in the threonine case study^a

solubility ^b	$c_{\star, \text{rac}} = k_{c1} + k_{c2}T + k_{c3}T^2$
	$k_{c1} \quad 5.139 \times 10^{-1}$
	$k_{c2} \quad 3.848 \times 10^{-3} \text{ K}^{-1}$
	$k_{c3} \quad 8.067 \times 10^{-6} \text{ K}^{-2}$
crystal growth ^c	$G = k_{g1} \exp\left(-\frac{k_{g2}}{T}\right) (S-1)^{k_{g3}} (1 + k_{g4}L)^{k_{g5}}$
	$k_{g1} \quad 4.968 \times 10^7 \text{ m s}^{-1}$
	$k_{g2} \quad 9.086 \times 10^3 \text{ K}$
	$k_{g3} \quad 1.192$
	$k_{g4} \quad 2.021 \times 10^4 \text{ m}^{-1}$
	$k_{g5} \quad 0.407$
primary nucleation ^{c,d}	$J_{\text{prim}} = k_{p1}T \exp\left(-\frac{k_{p2}}{T}\right) \sqrt{\frac{\rho_c}{c_{\star}}} (Sc_{\star})^{7/3} \exp\left(-\frac{k_{p3} \ln\left(\frac{\rho_c}{c_{\star}}\right)^3}{\ln(S)^2}\right)$
	$k_{p1} \quad 6.412 \times 10^{-7} \text{ kg}^{-1} \text{ s}^{-1}$
	$k_{p2} \quad 1.874 \times 10^3 \text{ K}$
	$k_{p3} \quad 4.300 \times 10^{-3}$
secondary nucleation ^{c,d}	$J_{\text{sec}} = k_{s1} \exp\left(-\frac{k_{s2}}{T}\right) (S-1)^{k_{s3}} (\mu_3)^{k_{s4}}$
	$k_{s1} \quad 2.380 \times 10^{23} \text{ kg}^{-1} \text{ s}^{-1}$
	$k_{s2} \quad 7.677 \times 10^3 \text{ K}$
	$k_{s3} \quad 4.800$
	$k_{s4} \quad 3.026$
dissolution	$D = k_d (S-1)$
	$k_d \quad 1.00 \times 10^{-6} \text{ m s}^{-1}$
daughter distribution	$d(\lambda, L) = 3L^2(2k_{b1} + 1) \left(\frac{2}{\lambda^3}\right)^{2k_{b1}+1} \left(L^3 - \frac{\lambda^3}{2}\right)^{2k_{b1}}$
	$k_{b1} \quad 7$
breakage rate	$K(L) = k_{b2}L^{k_{b3}}$
	$k_{b2} \quad 8 \times 10^{-4} \text{ kg}^{-1} \text{ s}^{-1}$
	$k_{b3} \quad 1$
shape factor, k_v	0.122
crystal density, ρ_c	1250 kg m^{-3}

^a All expressions made consistent with dimensions used in this paper.

^b Expression fitted through data points reported by Sapoundjiev et al. ³⁴.

^c Simplified from original expression reported in Qamar et al. ²⁴.

^d Note that $J = J_{\text{prim}} + J_{\text{sec}}$.

Table 2: Specification of processing parameters for case study 1

Quantity	Value
m_{C1}	10 kg
m_{M1}	1 kg
T_{C1}	283 K
T_{M1}	298 K
\dot{m}_{SC1}	$1 \times 10^{-3} \text{ kg s}^{-1}$
w_{SC1}^R	0.2
w_{SC1}^S	0.2
\dot{m}_{C1M1}	$3 \times 10^{-3} \text{ kg s}^{-1}$
\dot{m}_{C1F1}	$7.63 \times 10^{-3} \text{ kg s}^{-1}$
\dot{m}_{C1C2}	$2.21 \times 10^{-1} \text{ kg s}^{-1}$

Table 3: Specification of processing parameters for simulations involving enriched feed streams

Quantity	Value
m_{C1}	10 kg
m_{M1}	1 kg
m_{C2}	$s m_{C1}$
m_{M2}	$s m_{M1}$
T_{C1}	283 K
T_{M1}	298 K
T_{C2}	283 K
T_{M2}	298 K
\dot{m}_{SC1}	$1 \times 10^{-3} \text{ kg s}^{-1}$
\dot{m}_{SC2}	0 kg s^{-1}
w_{SC1}^R	0.2
w_{SC1}^S	varies (cf. Eq. (14))
\dot{m}_{C1M1}	$3 \times 10^{-3} \text{ kg s}^{-1}$
\dot{m}_{C2M2}	$s \dot{m}_{C1M1}$
\dot{m}_{C1F1}	$5.26 \times 10^{-3} \text{ kg s}^{-1}$
\dot{m}_{C2F2}	$s \dot{m}_{C1F1}$
\dot{m}_{C1C2}	$s \times 2.21 \times 10^{-1} \text{ kg s}^{-1} + s \dot{m}_{SC1}$
\dot{m}_{C2C1}	$s \times 2.21 \times 10^{-1} \text{ kg s}^{-1}$